

Electroweak baryogenesis in the three-loop radiative seesaw model with dark matter

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Based on [JHEP06(2025)036] and recent work

Introduction

Higgs was found in 2012, but **the structure of Higgs sector is still unknown.**

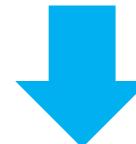
The number of Higgs field, representation, symmetry, …

Physics of electroweak symmetry breaking, details of phase transition

Related to BSM phenomena

ν oscillation
Dark matter
Baryon asymmetry

Testable with various experiments



Approaching new physics from Higgs physics

Q. Can we explain these 3 BSM phenomena simultaneously at TeV scale?

M. Aoki, S. Kanemura and O. Seto (2009)

→**We focus on Aoki-Kanemura-Seto (AKS) model**

Our purpose and work

M. Aoki, S. Kanemura and O. Seto (2009)

We evaluate baryon asymmetry based on original AKS model to explain 3 BSM phenomena

We search for parameter space which can explain 3 BSM phenomena simultaneously and test with various experiments

- Electron electric dipole moment (EDM)
- Lepton flavor violation
- Dark matter

----- [JHEP06(2025)036]

- Strongly 1st order electroweak phase transition(EWPT), Baryon number
- Find benchmark point which can explain 3 phenomena
- Test with various experiments (collider, GW, DM, neutrinos, EDMs, ...)

We show this model can explain 3 BSM phenomena while considering various constraints

Particle content

SM + **Extended Higgs** + **Right-handed ν**

- **Extended Higgs** → additional Higgs doublet ϕ_2 + singlet η , S^+
- **Right-handed neutrino** N_R^α $\alpha = 1,2,3$
- **Softly broken \tilde{Z}_2 symmetry** → suppress Flavor Changing Neutral Current
- **Exact Z_2 symmetry** → η, S^+, N_R^α are odd

Type-X 2HDM + N_R^α, S^\pm, η

$$\mathcal{L} \supset -\frac{\lambda_5}{2}(\phi_1^\dagger \phi_2)^2 - h_i^\alpha \overline{(N_R^\alpha)^c} l_R^i S^+ + \text{h.c.}$$

CP phase θ_5 ($\lambda_5 = |\lambda_5| e^{i\theta_5}$)

$\alpha = 1,2,3, i = 1,2,3, h_i^\alpha$ is 3×3 complex matrix

	Z_2	\tilde{Z}_2 (Softly broken)
ϕ_1	+	+
ϕ_2	+	-
N_R^α	-	-
S^+	-	+
η	-	-

Dark matter →

Aoki-Kanemura-Seto model

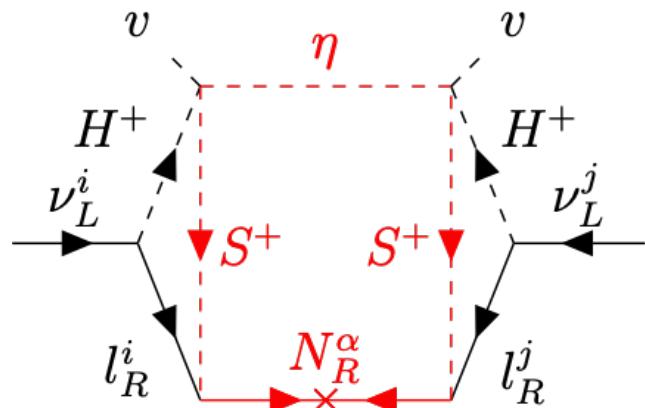
Aoki-Kanemura-Seto (AKS) model can explain 3 BSM phenomena simultaneously at TeV scale

M. Aoki, S. Kanemura and O. Seto (2009)

Z_2 symmetry $\begin{cases} \text{Tiny } \nu \text{ mass via radiative correction} \\ \text{Dark matter candidate } (\mathbb{Z}_2 \text{ odd neutral particle}) \end{cases}$

Baryon asymmetry : **Electroweak baryogenesis (EWBG)**

Energy scale : **TeV \rightarrow Testable at collider**



$$M_{ij} \sim \left(\frac{1}{16\pi^2} \right)^3 \times \left(\frac{m_l}{v} \right)^2 \times \frac{v^2}{m_N} < \text{eV}$$

$\sim 10^{-6}$ $\sim 10^{-4}$

3-loop neutrino mass generation

	Z_2	\tilde{Z}_2 for FCNC	\tilde{Z}_2 (Softly broken)
ϕ_1	+		+
ϕ_2	+		-
N_R^α	-		-
S^+	-		+
η	-		-

Dark matter

$$V \supset + \sum_{a=1}^2 \left(\rho_a |\phi_a|^2 |S^+|^2 + \frac{1}{2} \sigma_a |\phi_a|^2 \eta^2 \right)$$

DM-Higgs interaction

η : Dark matter

Dominant contribution to the relic density

$\tan \beta = 18$

$$(\sigma_1 \sin^2 \beta + \sigma_2 \cos^2 \beta) \simeq \sigma_1$$

$$\sigma_1 = 0.0841$$

$$\rightarrow \Omega h^2 \simeq 0.12$$

DM direct detection

spin-independent cross section for $\eta N \rightarrow \eta N$

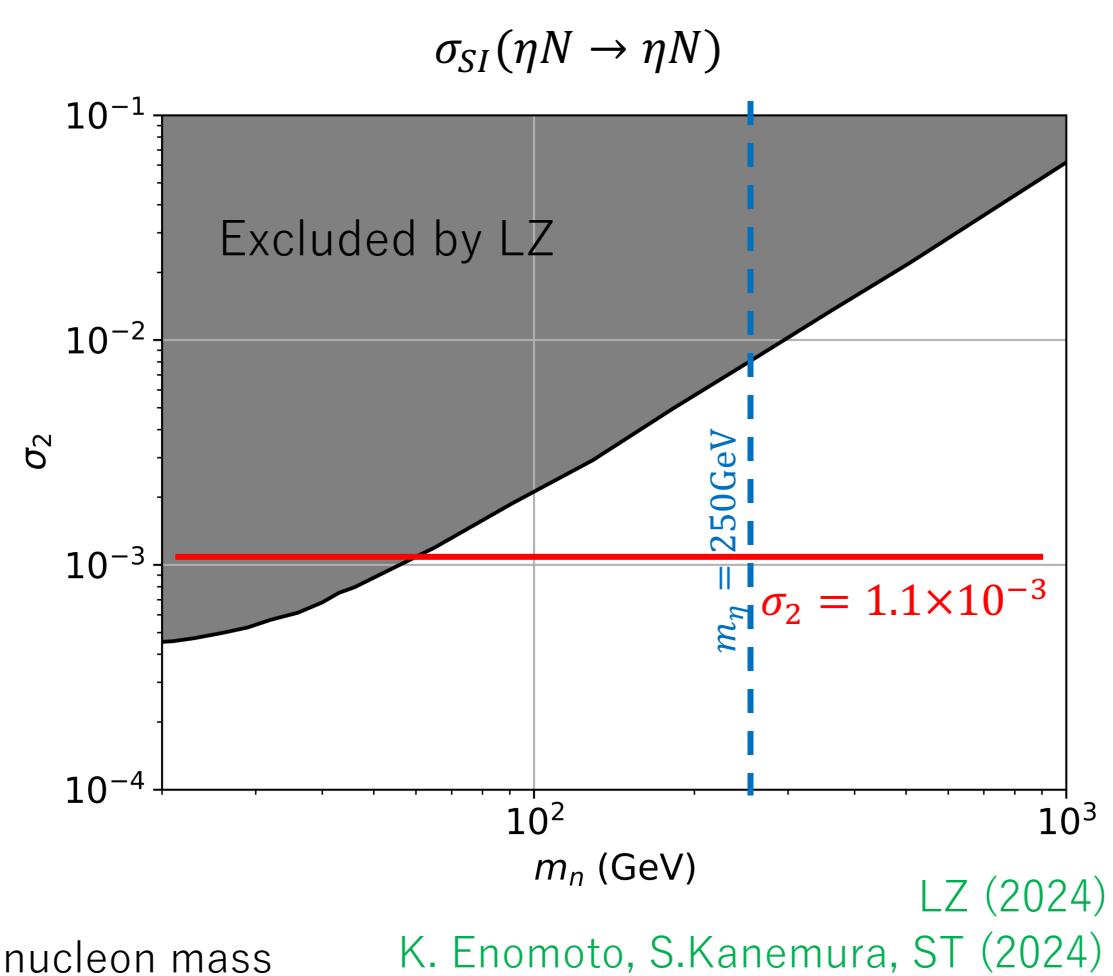
$$\sigma_{\text{SI}} \simeq \frac{g^2 m_N^2 v^2}{4\pi(m_\eta + m_N)^2 m_{H_1}^4} (\sigma_1 \cos \beta + \sigma_2 \sin \beta)^2$$

$m_N \simeq 1 \text{ GeV}$: nucleon mass

$g \simeq 10^{-3}$: coupling for nucleon-Higgs

Shifman, et al (1978)

$$(\sigma_1 \cos \beta + \sigma_2 \sin \beta) \simeq \sigma_2$$



Electroweak Baryogenesis

Electroweak Baryogenesis

Kuzmin, Rubakov and Shaposhnikov (1985)

- (1) B violation
- (2) C, CP violation
- (3) Departure from thermal equilibrium

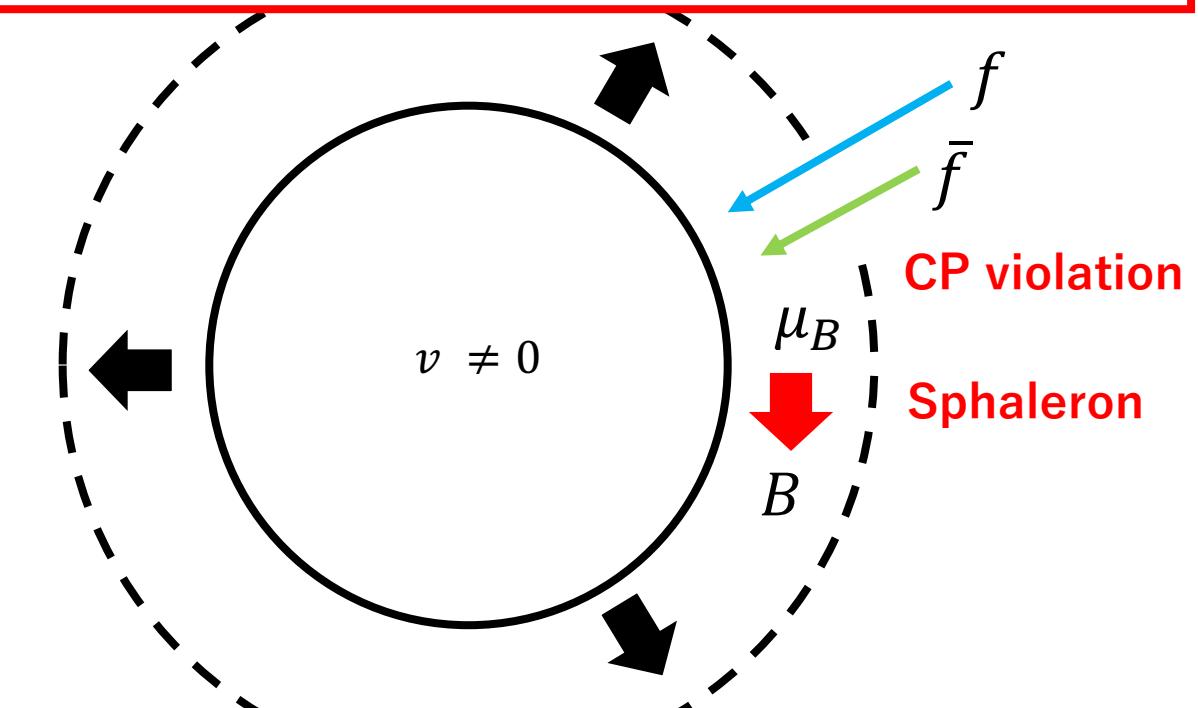
Sakharov (1967)

→ Sphaleron Transition
→ CP violation in extended Higgs sector
→ Sphaleron decoupling
→ Strongly 1st order EWPT

Charges accumulate around the bubble wall due to the CPV

↓
B number is generated by sphaleron

↓
Sphaleron decouples inside the bubble wall and B number remains



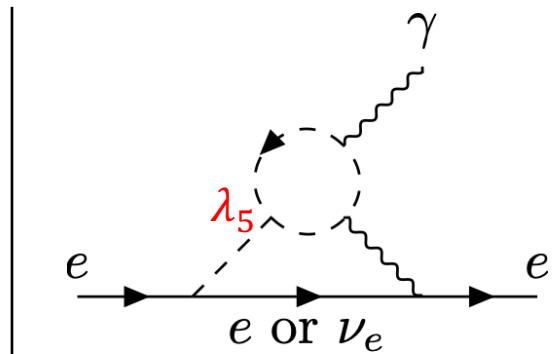
Electric dipole moment in our model

Sufficient CP phase ($\theta_5 \sim O(1)$) for EWBG is severely constrained by electron EDM experiments ($|d_e| < 4.1 \times 10^{-30}$ ecm).

Roussy et al. (JILA) (2023)

$$\mathcal{L} \supset - [h_i^\alpha \overline{(N_R^\alpha)^c} l_R^i S^+ + \text{h.c.}]$$

Electron EDM can be small by considering following contribution

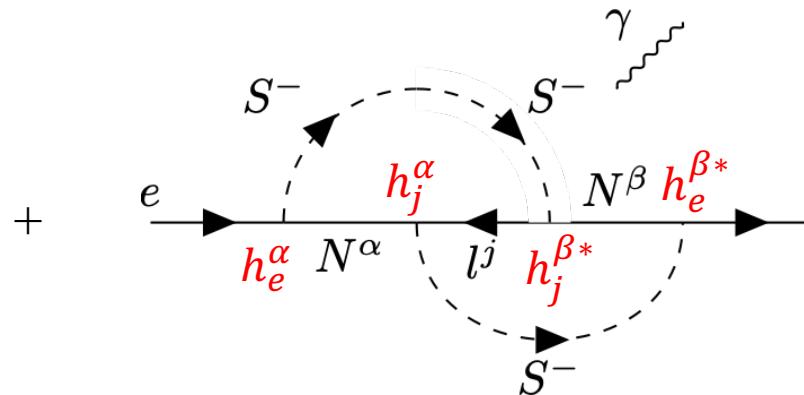


Barr, Zee (1990)
Altmannshofer, et al (2020)

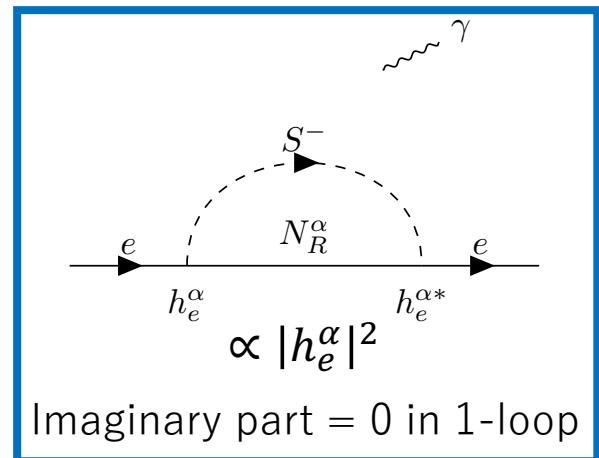
Contribution in 2HDM
(Barr-Zee contribution)

$$|d_e| \simeq 8.3 \times 10^{-31} \text{ ecm} < 4.1 \times 10^{-30} \text{ ecm}$$

$$\theta_5 \simeq -0.090\pi$$



Additional contribution
in CPV AKS model



Strongly 1st Order Phase Transition

Sphaleron decoupling $\rightarrow \Gamma_{sph}^{br} < H(T_c)$

→ **Strongly 1st order EWPT** $\frac{\varphi_c}{T_c} > 1$

Γ_{sph}^{br} : Sphaleron rate in broken phase
 $H(T_c)$: Hubble const. at transition temp.

→ non-decoupling effects of additional scalars

This effect gives a large deviation in hhh coupling

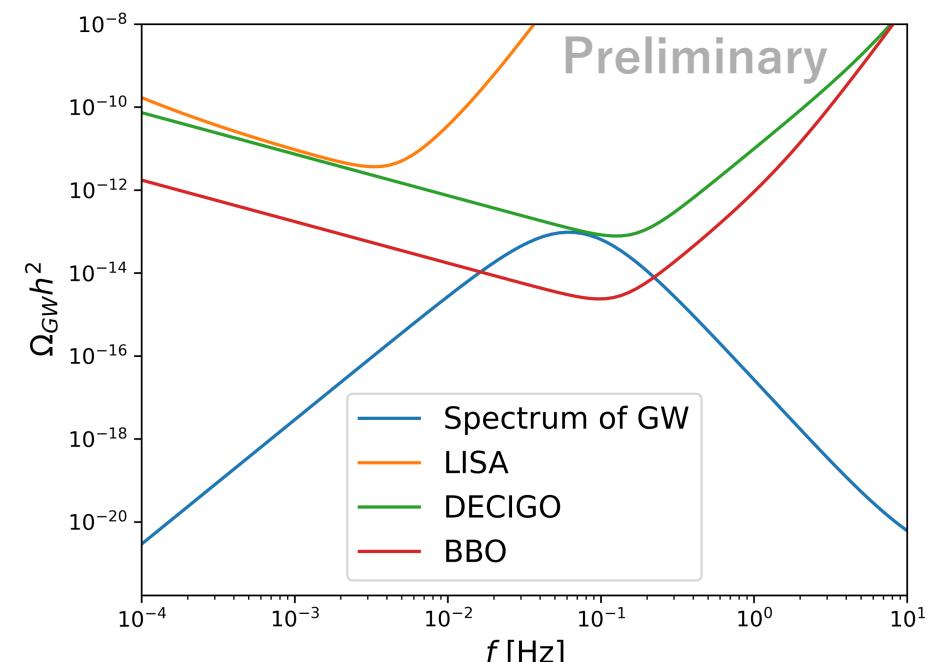
Kanemura, Kiyoura, Okada, Senaha, Yuan (2002)

Kanemura, Okada, Senaha, Yuan (2004)

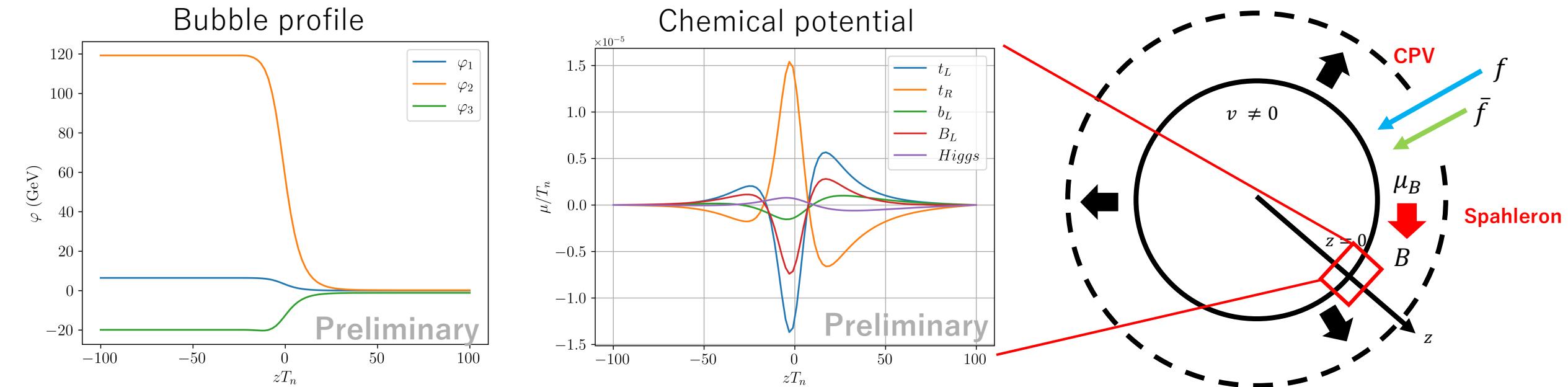
$$\Delta R \equiv \frac{\lambda_{hhh} - \lambda_{hhh}^{SM}}{\lambda_{hhh}^{SM}} \simeq 36\%$$

GW from strongly 1st order EWPT

→ testable at BBO, DECIGO



Baryon asymmetry



Top transport scenario with WKB approx.

CosmoTransition

Wainwright (2011)

Cline, Joyce, Kainulainen (2000)

Fromme, Huber (2006)

Cline, Kainulainen (2020)

Chemical potential outside the wall convert to baryon asymmetry by Sphaleron

Observed : $\eta_B = \frac{n_B}{n_\gamma} = (6.04 - 6.20) \times 10^{-10}$ From CMB Planck (2018)

$$\eta_B \simeq 6.07 \times 10^{-10}$$

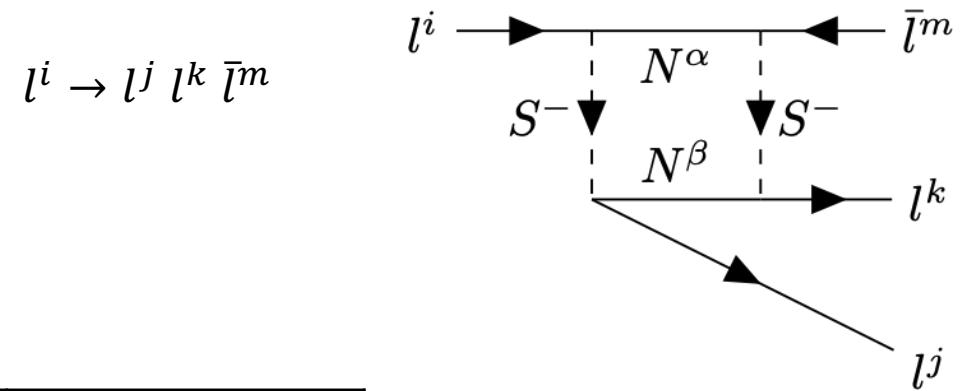
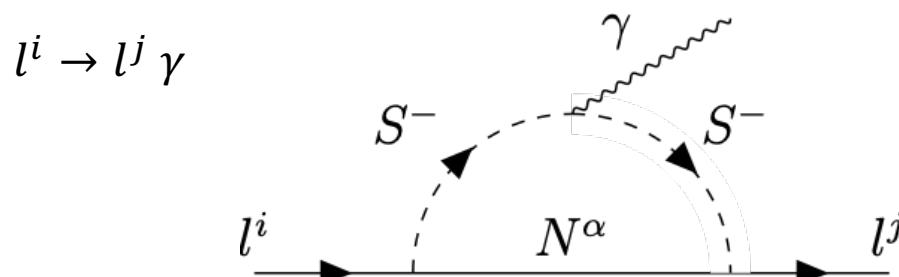
$$m_{H^1} \simeq 125 \text{ GeV}, m_{H^2} \simeq 207 \text{ GeV},$$

$$m_{H^3} = m_{H^\pm} \simeq 373 \text{ GeV}$$

$$M \simeq 210 \text{ GeV}, m_S = 325 \text{ GeV},$$

$$\mu_S = 20 \text{ GeV}, \theta_5 \simeq -0.090\pi$$

Lepton flavor violation



K. Enomoto, S.Kanemura, ST (2024)

	Prediction	Exp. bounds
$\mu \rightarrow e\gamma$	2.3×10^{-14}	3.1×10^{-13}
$\tau \rightarrow e\gamma$	1.8×10^{-11}	3.3×10^{-8}
$\tau \rightarrow \mu\gamma$	2.0×10^{-17}	4.4×10^{-8}
$\mu \rightarrow 3e$	1.0×10^{-13}	1.0×10^{-12}
$\tau \rightarrow 3e$	3.1×10^{-12}	2.7×10^{-8}
$\tau \rightarrow 3\mu$	2.6×10^{-23}	2.1×10^{-8}
$\tau \rightarrow e\mu\bar{e}$	3.1×10^{-17}	1.8×10^{-8}
$\tau \rightarrow \mu\mu\bar{e}$	1.4×10^{-17}	1.7×10^{-8}
$\tau \rightarrow e\mu\bar{\mu}$	8.3×10^{-19}	2.7×10^{-8}

MEG-II(2024)

BaBar(2010)

BaBar(2010)

Mu3e(2023)

BaBar(2010)

Belle (2010)

Belle (2010)

Belle (2010)

Belle (2010)

Phenomenology in collider experiments

S^\pm Production

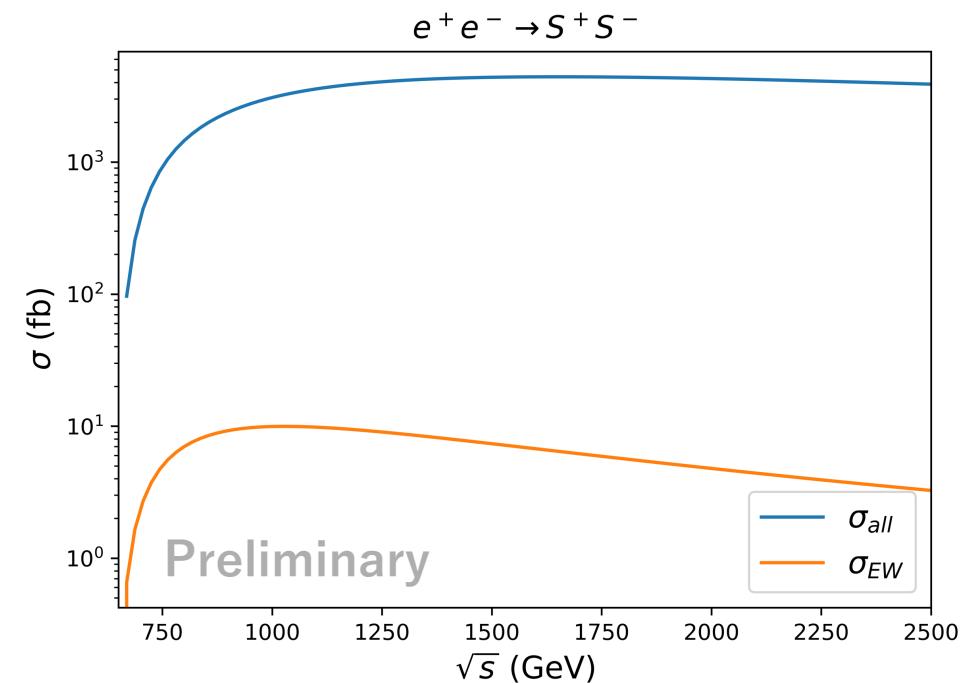
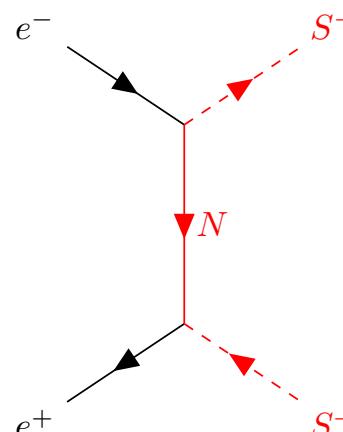
Production : Drell-Yan process
t-channel process
(lepton collider)

$S^+ \rightarrow H^\pm \eta \rightarrow \tau \nu \eta$ is the main decay channel
 $e^+ e^- \rightarrow S^+ S^- \rightarrow \tau \bar{\tau} E$ (E : missing energy)

LHC can produce S^\pm by Drell-Yan process

Additional Higgs H_2, H_3 can be tested at future HL-LHC by

$$H_2, H_3 \rightarrow \tau \bar{\tau}, t \bar{t} \quad H_2, H_3 \rightarrow Z H_1, H_1 H_1$$



$pp \rightarrow S^+ S^-$ (MadGraph)

$$\sqrt{s} = 13 \text{ TeV} : \sigma = 0.976 \text{ fb}$$

$$\sqrt{s} = 14 \text{ TeV} : \sigma = 1.14 \text{ fb}$$

Summary

- AKS model can explain 3 BSM phenomena simultaneously at the TeV scale.
- We introduce CP violation into the original AKS model (2009).
- We evaluate the baryon number and confirm that it can explain current observed data.
- We find the benchmark point to explain 3 BSM phenomena while avoiding several constraints.
- Prospects
 - Test with various experiments (collider, flavor, DM, neutrinos, EDMs, GW, ...)

Back up

Test of our benchmark scenario

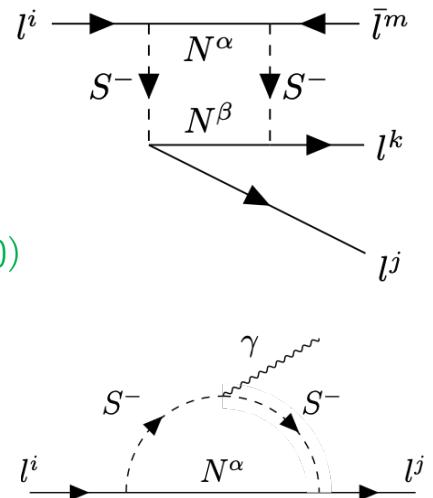
LFV

	Prediction	Exp. bound	Expected sensitivity
$\mu \rightarrow e\gamma$	2.3×10^{-15}	3.1×10^{-13}	6×10^{-14}
$\mu \rightarrow 3e$	1.0×10^{-13}	1.0×10^{-12}	1×10^{-16}
$\tau \rightarrow 3e$	3.1×10^{-12}	2.7×10^{-8}	4×10^{-10}

MEG-II(2018)

Mu3e phase-II(2020)

Belle-II(2018)



Electron EDM

Future ACME-III aim : $|d_e| < 10^{-30}$ ecm

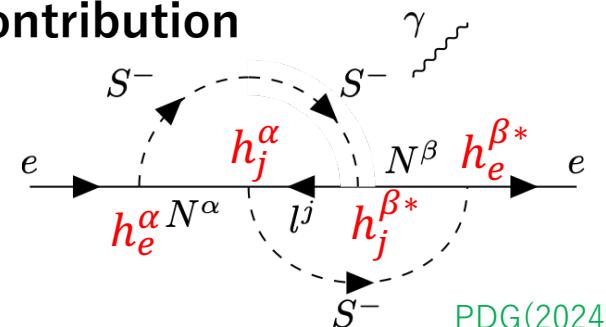
$$|d_e| \simeq 8.3 \times 10^{-31} \text{ ecm}$$

Neutron, proton EDM

$$\tan \beta = 18$$

Quark Yukawa couplings are suppressed by $\cot \beta$

Lepton contribution



EDM cancellation does not work for neutron, proton EDMs
 → Future neutron, proton EDM can test CP violation

$$|d_n| < 1.8 \times 10^{-26} \text{ ecm}$$

$$|d_p| < 2.1 \times 10^{-25} \text{ ecm}$$

PDG(2024)

Lagrangian

Type-X 2HDM + N_R^α, S^\pm, η

Higgs potential

$$\begin{aligned}
 V = & -\mu_1^2 |\phi_1|^2 - \mu_2^2 |\phi_2|^2 - (\boxed{\mu_{12}^2} \phi_1^\dagger \phi_2 + \text{h.c.}) + \mu_S^2 |S|^2 + \frac{\mu_\eta^2}{2} \eta^2 + \frac{\lambda_1}{2} |\phi_1|^4 + \frac{\lambda_2}{2} |\phi_2|^4 \\
 & + \lambda_3 |\phi_1|^2 |\phi_2|^2 + \lambda_4 |\phi_1^\dagger \phi_2|^2 + \left(\frac{\lambda_5}{2} (\phi_1^\dagger \phi_2)^2 + \text{h.c.} \right) + \frac{\lambda_S}{4} |S|^4 + \frac{\lambda_\eta}{4!} \eta^4 + \frac{\xi}{2} |S|^2 \eta^2 \\
 & + \sum_{a=1}^2 \left(\rho_a |\phi_a|^2 |S|^2 + \frac{1}{2} \sigma_a |\phi_a|^2 \eta^2 \right) + (2 \boxed{\kappa} \tilde{\phi}_1^\dagger \phi_2 S^- \eta + \text{h.c.})
 \end{aligned}$$

Stationary cond. $\text{Im} [\mu_{12}^2] - \frac{1}{2} \text{Im} [\lambda_5] v_1 v_2 = 0$
 $\rightarrow \mu_{12}^2, \lambda_5$ are not independent

CP phase θ_5 ($\lambda_5 = |\lambda_5| e^{i\theta_5}$)

Phase of κ will vanish by rephasing of S^-

The physical CP phase in Higgs potential is only θ_5

Neutrino Yukawa

$$\mathcal{L} \supset - \boxed{h_i^\alpha} \overline{(N_R^\alpha)^c} l_R^i S^+ + \text{h.c.} \quad \alpha = 1, 2, 3, \quad i = 1, 2, 3, \quad h_i^\alpha : 3 \times 3 \text{ complex matrix}$$

CP violation (CP phase ψ_1, ψ_2, ψ_3 + PMNS phase $\delta, \alpha_1, \alpha_2$)

Benchmark scenario

$$m_{H^1} \simeq 125 \text{ GeV}, m_{H^2} \simeq 207 \text{ GeV}, m_{H^3} = m_{H^\pm} \simeq 373 \text{ GeV}$$

$$M \simeq 210 \text{ GeV}, m_S = 325 \text{ GeV}, m_\eta = 250 \text{ GeV}$$

$$(m_{N^1}, m_{N^2}, m_{N^3}) = (400, 900, 1400) \text{ GeV}$$

$$\sigma_1 = 0.0841, \sigma_2 = 1.1 \times 10^{-3}$$

$$m_{\nu^1} = 8.1 \text{ meV}, \kappa \tan \beta = 45, \tan \beta = 18, \theta_5 \simeq -0.090\pi$$

$$h_i^\alpha \simeq \begin{pmatrix} 1.3e^{-0.16\pi i} & 0.0028e^{-0.90\pi i} & 0.011e^{-0.042\pi i} \\ 0.51e^{-0.36\pi i} & 0.039e^{-0.0055\pi i} & 0.0039e^{-0.35\pi i} \\ 1.4e^{-0.45\pi i} & 0.015e^{-9.8\pi i} & 0.0076e^{-0.58\pi i} \end{pmatrix}$$

Transport equation

$$\begin{cases} -D_{1t}\mu'_t + u'_t + \gamma v_w(m_t^2)'Q_{2t}\mu_t - K_{0t}\bar{\Gamma}_t = -S_{1t}, \\ -D_{2t}\mu'_t - v_wu'_t + \gamma v_w(m_t^2)'Q_{t2}\mu_t + (m_t^2)'\bar{R}_tu_t + \Gamma_{t,\text{tot}}u_t + v_wK_{0t}\bar{\Gamma}_t = -S_{2t}. \end{cases}$$

$$\begin{cases} -D_{1b}\mu'_b + u'_b - K_{0b}\bar{\Gamma}_b = 0, \\ -D_{2b}\mu'_b - v_wu'_b + \Gamma_{b,\text{tot}}u_b + v_wK_{0b}\bar{\Gamma}_b = 0. \end{cases}$$

$$\begin{cases} -D_{1t}\mu'_{t^c} + u'_{t^c} + \gamma v_w(m_t^2)'Q_{2t}\mu_{t^c} - K_{0t}\bar{\Gamma}_{t^c} = -S_{1t}, \\ -D_{2t}\mu'_{t^c} - v_wu'_{t^c} + \gamma v_w(m_t^2)'Q_{t2}\mu_{t^c} + (m_t^2)'\bar{R}_tu_{t^c} + \Gamma_{t,\text{tot}}u_{t^c} + v_wK_{0t}\bar{\Gamma}_{t^c} = -S_{2t}. \end{cases}$$

$$\begin{cases} -D_{1h}\mu'_h + u'_h - K_{0h}\bar{\Gamma}_h = 0, \\ -D_{2h}\mu'_h - v_wu'_h + \Gamma_{h,\text{tot}}u_h + v_wK_{0h}\bar{\Gamma}_h = 0. \end{cases}$$

$$S_{li} = -\gamma v_w(m_i^2\theta'_i)'Q_{li}^8 + \gamma v_w m_i^2 \theta'_i (m_i^2)'Q_{li}^9, \quad (l=1,2).$$

Collision rate

$$\begin{aligned}\bar{\Gamma}_t &= \Gamma_{ss} \left((1 + 9D_{0t})\mu_t + 10\mu_b + (1 - 9D_{0t})\mu_{t^c} \right) \\ &\quad + \Gamma_W(\mu_t - \mu_b) + \Gamma_y(\mu_t + \mu_{t^c} + \mu_h) + 2\Gamma_m(\mu_t + \mu_{t^c}), \\ \bar{\Gamma}_b &= \Gamma_{ss} \left((1 + 9D_{0t})\mu_t + 10\mu_b + (1 + 9D_{0t})\mu_{t^c} \right) \\ &\quad + \Gamma_W(\mu_b - \mu_t) + \Gamma_y(\mu_b + \mu_{t^c} + \mu_h), \\ \bar{\Gamma}_{t^c} &= \Gamma_{ss} \left((1 + 9D_{0t})\mu_t + 10\mu_b + (1 - 9D_{0t})\mu_{t^c} \right) \\ &\quad + 2\Gamma_m(\mu_{t^c} + \mu_t) + \Gamma_y(2\mu_{t^c} + \mu_t + \mu_b + 2\mu_h), \\ \bar{\Gamma}_h &= \frac{3}{4}\Gamma_y(2\mu_h + \mu_t + \mu_b + 2\mu_{t^c}) + \Gamma_h\mu_h.\end{aligned}$$

Baryon asymmetry

$$\mu_{B_L} = \frac{1}{2}(1 + 4D_{0t})\mu_t + \frac{1}{2}(1 + 4D_{0b})\mu_b - 2D_{0t}\mu_{t^c}.$$

$$\eta_B = \frac{405\Gamma_{\rm sph}}{4\pi^2 v_w g_* T_n} \int_0^\infty dz ~ \mu_{B_L} f_{\rm sph}(z) \exp\left(-\frac{45\Gamma_{\rm sph} z}{4v_w}\right),$$

$$f_{\rm sph}(z) = \min\biggl\{1,~\frac{2.4T}{\Gamma_{\rm sph}}e^{-\frac{40v_n(z)}{T}}\biggr\}.$$

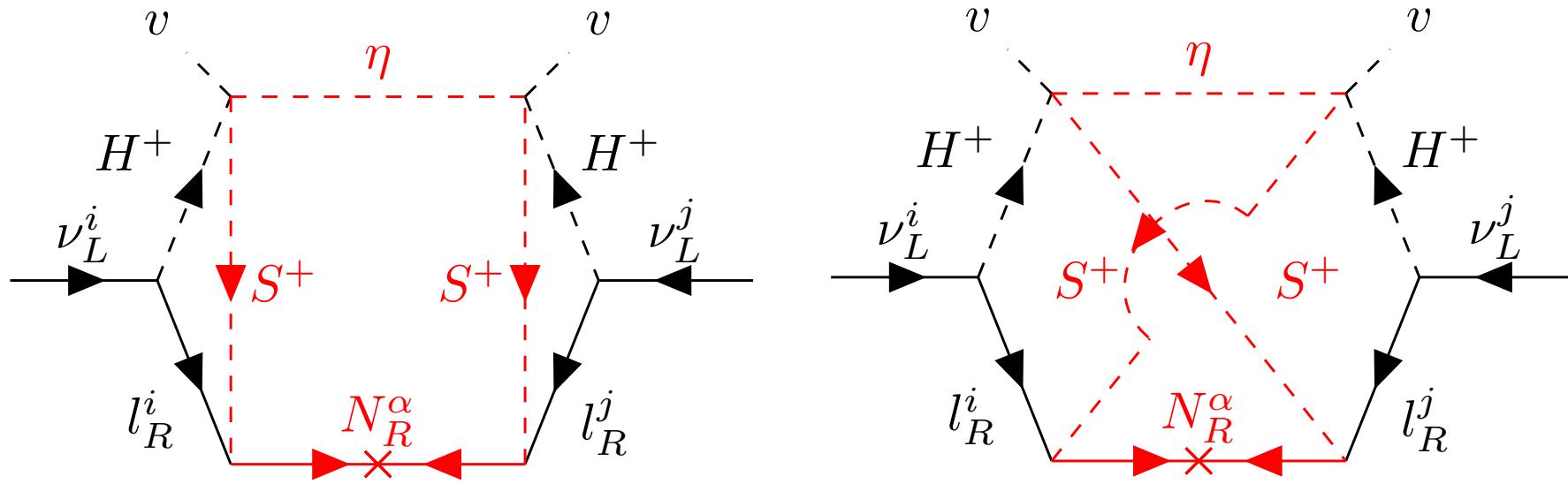
Casas-Ibarra parametrization

$$h = \frac{(16\pi^2)^{\frac{3}{2}}}{|\kappa \tan \beta|} \sqrt{\Lambda} R \sqrt{D} U_{\text{PMNS}}^\dagger (M_L^{-1})$$

$$\Lambda_{\alpha\beta} = \frac{1}{m_\alpha(F_{1\alpha} + F_{2\alpha})} \delta_{\alpha\beta} \quad D \equiv \text{diag}(m_{\nu^1}, m_{\nu^2}, m_{\nu^3}) \quad M_L = \text{diag}(m_e, m_\mu, m_\tau)$$

$$R = \frac{1}{c_{\psi_1} c_{\psi_2} c_{\psi_3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{\gamma_1} & s_{\gamma_1} \\ 0 & -s_{\gamma_1} & c_{\gamma_1} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & i s_{\psi_1} \\ 0 & -i s_{\psi_1} & 1 \end{pmatrix} \begin{pmatrix} c_{\gamma_2} & 0 & s_{\gamma_2} \\ 0 & 1 & 0 \\ -s_{\gamma_2} & 0 & c_{\gamma_2} \end{pmatrix} \\ \times \begin{pmatrix} 1 & 0 & i s_{\psi_2} \\ 0 & 1 & 0 \\ -i s_{\gamma_2} & 0 & 1 \end{pmatrix} \begin{pmatrix} c_{\gamma_3} & s_{\gamma_3} & 0 \\ -s_{\gamma_3} & c_{\gamma_3} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & i s_{\psi_3} & 0 \\ -i s_{\psi_3} & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Neutrino mass matrix



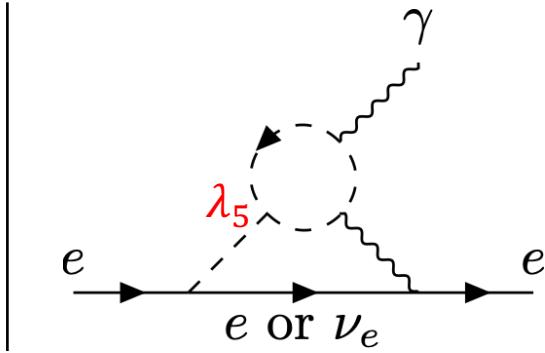
$$(M_\nu)_{ij} = \frac{(\kappa \tan \beta)^2 m_{l^i} m_{l^j}}{(16\pi^2)^3} \sum_{\alpha=1}^3 h_i^\alpha h_j^\alpha m_{N^\alpha} (F_{1\alpha} + F_{2\alpha})$$

$$F_{n\alpha} = \int \tilde{d}^4x \int_0^\infty du \int_0^\infty dv \frac{8\sqrt{uv}\tilde{F}(a_n, b_N)}{(u + m_{H^\pm}^2)(v + m_{H^\pm}^2)}$$

Yukawa interaction in Type-X 2HDM

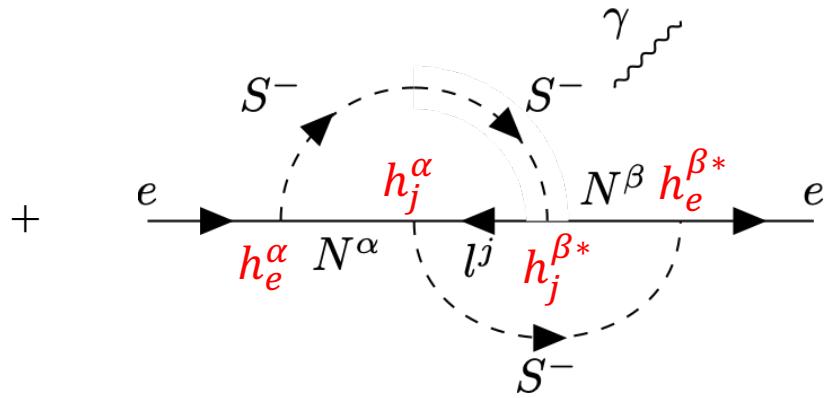
$$\begin{aligned}\mathcal{L}_y = & -m_{u^i} \bar{u}^i u^i - m_{d^i} \bar{d}^i d^i - m_{l^i} \bar{l}^i l^i \\ & - \sum_a H_a \left\{ \frac{m_{u^i}}{v} \bar{u}^i (R_{1a} + R_{2a} \cot \beta - i R_{3a} \cot \beta \gamma_5) u^i \right. \\ & \quad + \frac{m_{d^i}}{v} \bar{d}^i (R_{1a} + R_{2a} \cot \beta + i R_{3a} \cot \beta \gamma_5) d^i \\ & \quad \left. + \frac{m_{l^i}}{v} \bar{l}^i (R_{1a} + R_{2a} \tan \beta + i R_{3a} \tan \beta \gamma_5) l^i \right\} \\ & - \frac{\sqrt{2}}{v} \left\{ \cot \beta \bar{u}^i V_{ij} (m_{d^i} P_R - m_{u^i} P_L) d^j H^+ + \tan \beta m_{l^i} \bar{\nu}^i P_R l^i H^+ + \text{h.c.} \right\}\end{aligned}$$

Electric dipole moment in our model



Contribution in 2HDM
(Barr-Zee contribution)

$$-1.1232 \times 10^{-29} \text{ ecm}$$



Additional contribution
in CPV AKS model

$$1.1314 \times 10^{-29} \text{ ecm}$$

+

$$< 4.1 \times 10^{-30} \text{ ecm}$$

$$\mathbf{8.3 \times 10^{-31} \text{ ecm}}$$

Details of Benchmark scenario

$$R_h = \begin{pmatrix} 0.999898 & 0.00774 & 0.0120 \\ -0.00598 & 0.990 & -0.141 \\ 0.0130 & -0.141 & 0.98995 \end{pmatrix}$$

$$R_h^T M_h^2 R_h = \begin{pmatrix} 125 & 0 & 0 \\ 0 & 207 & 0 \\ 0 & 0 & 373 \end{pmatrix}^2$$

$$\lambda_1 \simeq 3.47$$

$$\lambda_2 \simeq 0.259$$

$$\lambda_3 \simeq 3.34$$

$$\lambda_4 \simeq -1.56$$

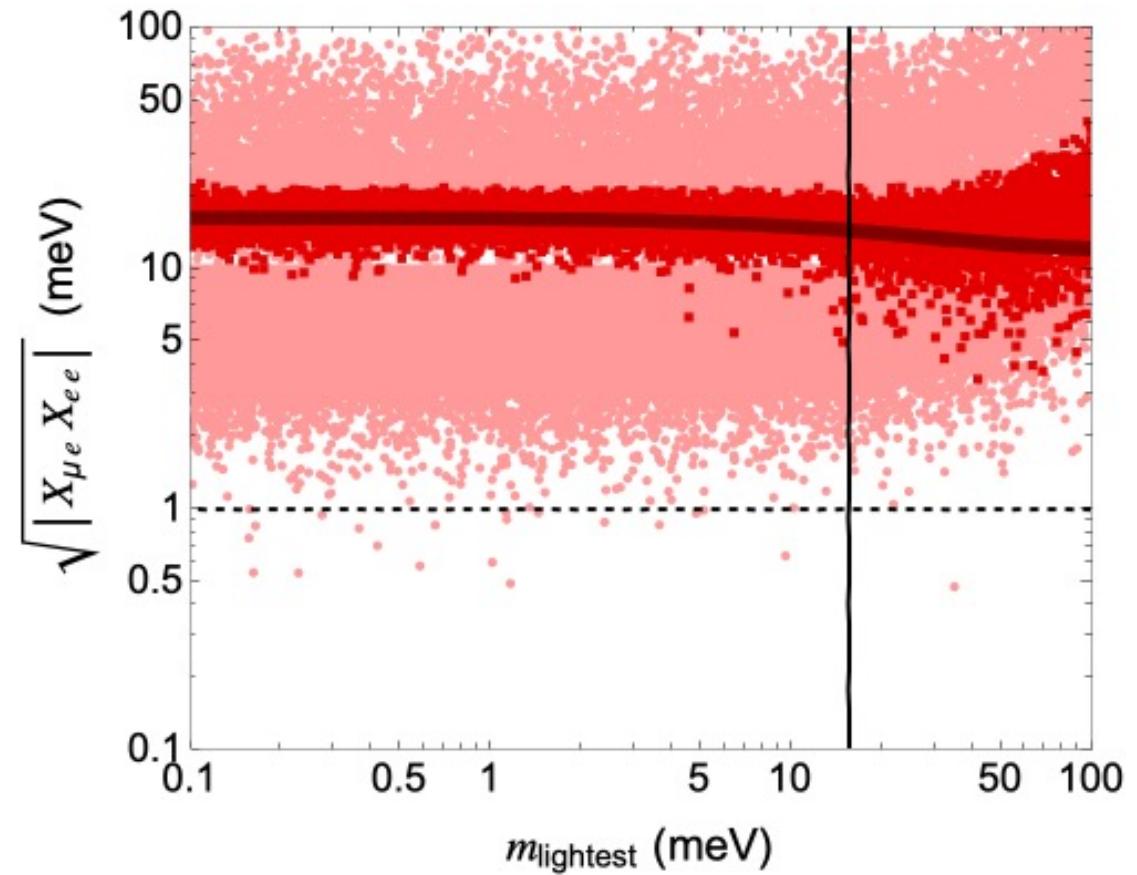
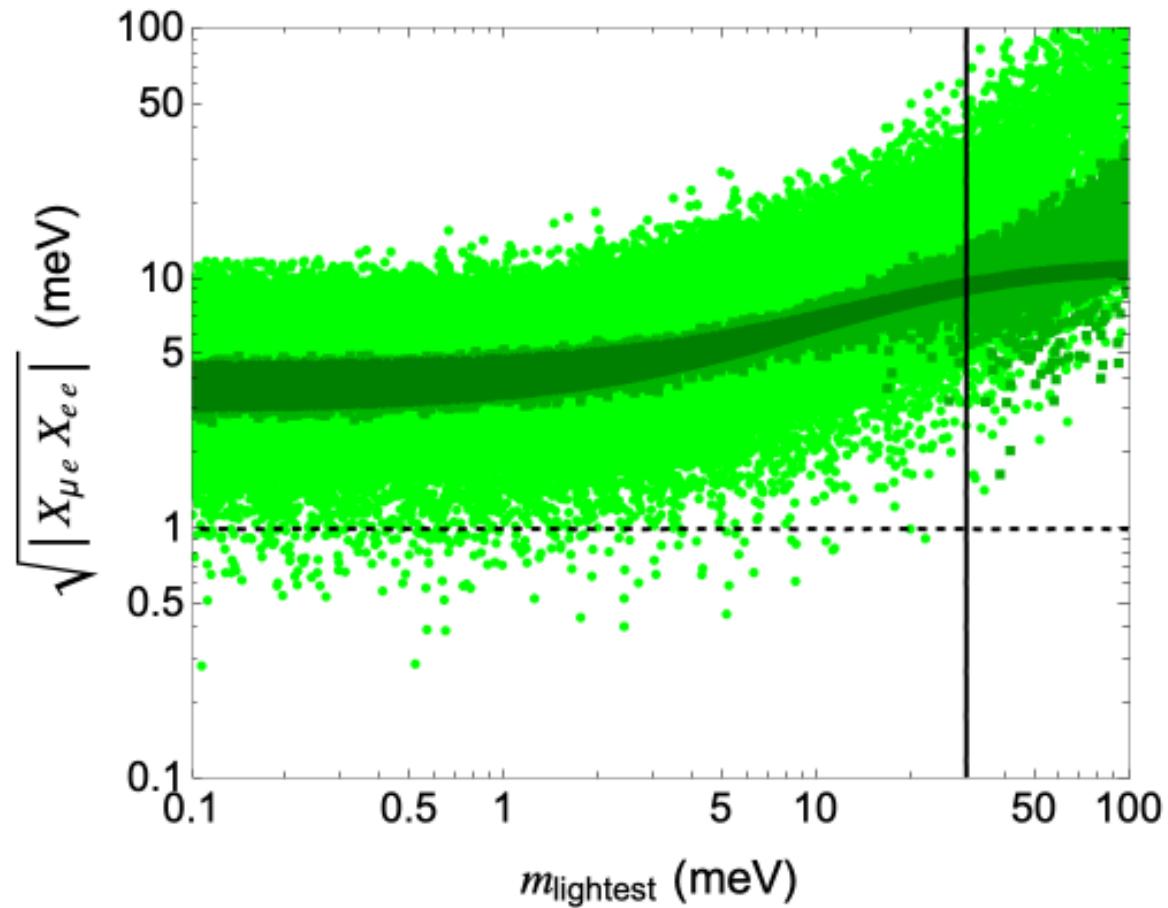
$$\lambda_5 \simeq -1.53 + 0.32i$$

$$S \simeq -0.012$$

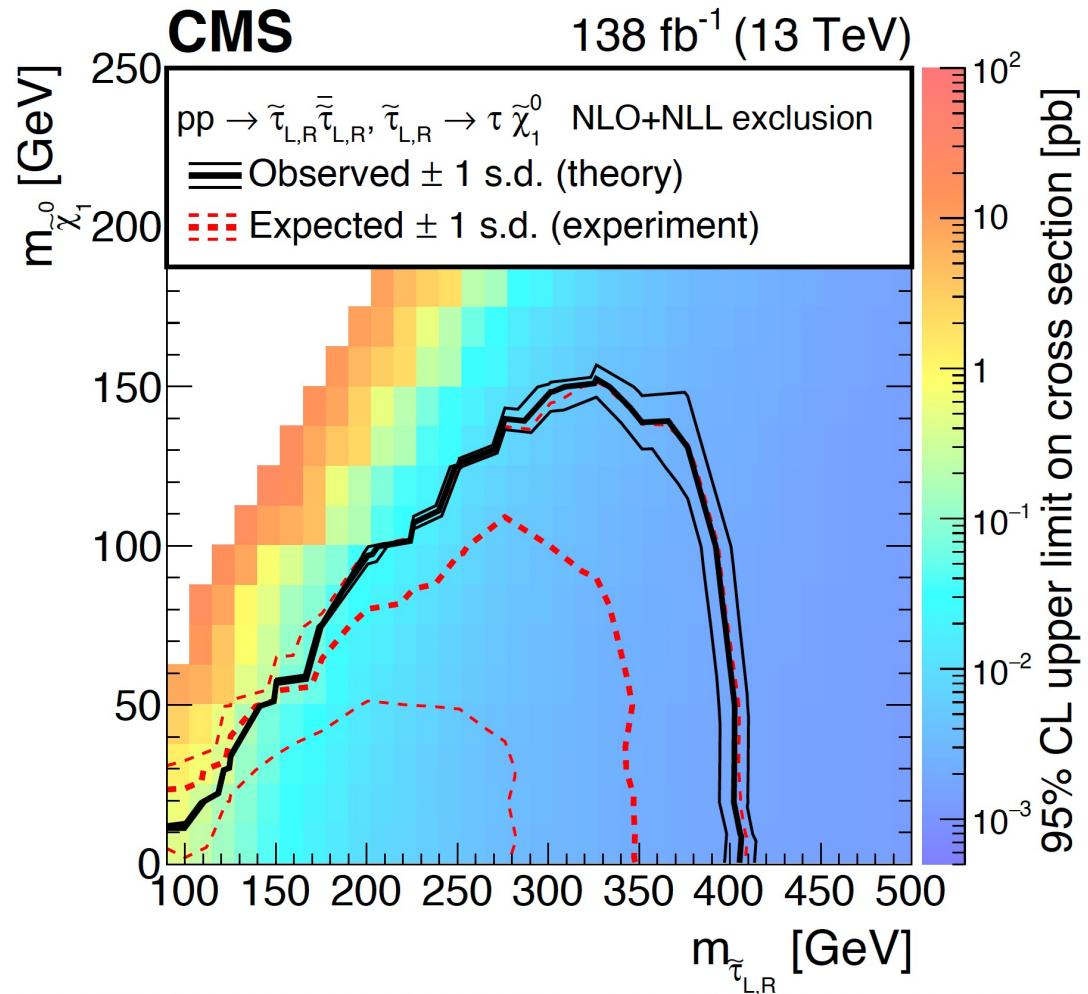
$$T \simeq 0$$

$$U \simeq -2.05 \times 10^{-5}$$

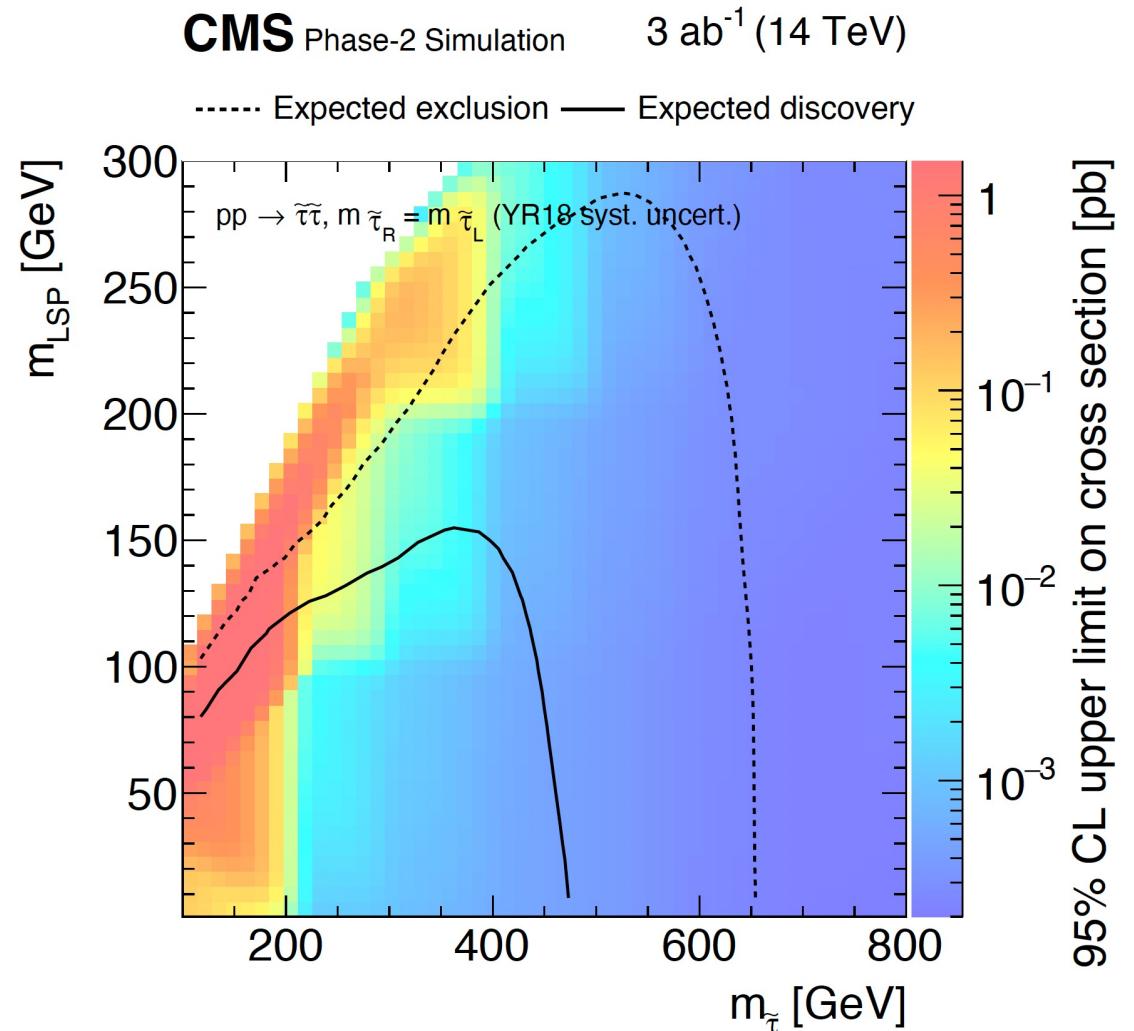
LFV constraint



Stau search



CMS (2022)



CMS (2019)

v_n/T_n

