# **Rarita-Schwinger Fields and Cosmology**



Sep 22 – 25, 2025 University of Warsaw, Faculty of Physics

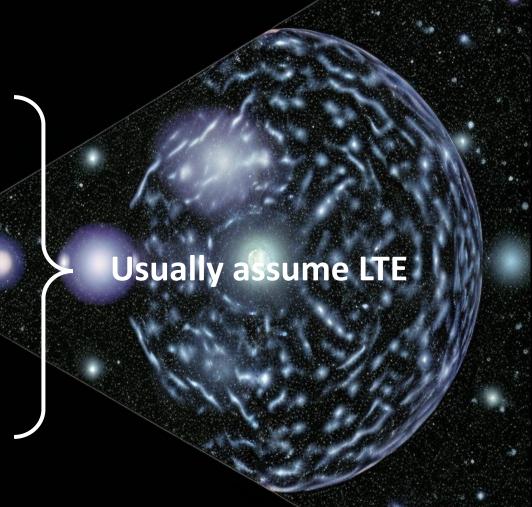




# Inner Space/Outer Space Interface

**Cosmological limits on particle properties:** 

- 1. neutrinos
- 2. axions
- 3. magnetic monopoles
- 4. all sorts of BSM particles (e.g., SUSY)
- 5. cosmological defects
- 6. Kaluza-Klein modes
- 7. String theorists suggest a lot of unseen things ... difficult to get rid of them

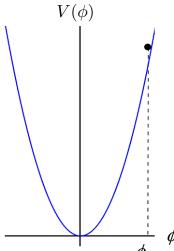


will consider limits from "cosmological gravitational particle production (CGPP)"

CGPP can populate hidden sectors & produce DM w/ only gravitational interactions

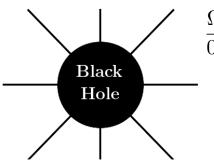
### Ideas for gravitational particle production

#### Misalignment



- Superhorizon quantum fluctuations during inflation
- After inflation, field frozen by "Hubble drag'' until H drops below mass
- Then energy density in oscillating field
- Most familiar example is the axion

#### Hawking radiation from primordial black holes Hooper, Krnjaic, & McDermott



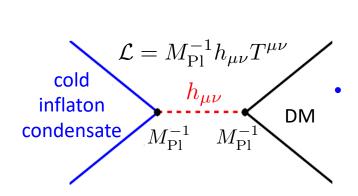
- $\frac{\Omega h^2}{0.12} \approx \left(\frac{10^{11} \text{GeV}}{m}\right) \left(\frac{10^{12} \text{GeV}}{T_i}\right)^3 \left(\frac{\epsilon_{\text{BH}}}{10^{-16}}\right)$ 
  - PBH seeds from inflation
  - PBHs evaporate in early universe
  - DM mass  $\sim 10^{11} \, \text{GeV}$  (WIMPzilla)

#### From primordial plasma via graviton exchange Garny, Sandora, & Sloth

$$\frac{\Omega h^2}{0.12} pprox \left(\frac{\langle \sigma v \rangle}{T^2/M_{\rm Pl}^4}\right) \left(\frac{m}{10^{13} {\rm GeV}}\right) \left(\frac{T_{\rm RH}}{10^{14} {\rm GeV}}\right)^3$$

- plasma
- Reheating produces SM plasma
- DM DM mass  $\sim 10^{13}\,\mathrm{GeV}$  (WIMPzilla) Assumes  $m < T_\mathrm{RH}$

#### From inflaton field after inflation via graviton exchange Ema, Nakayama, Tang; Mambrini & Olive



- "Boltzmann" approach not complete treatment (Kaneta, Lee, Oda; Basso, Chung, EWK, Long).
  - Underestimates particle production: must include Schrödinger Effect (production during quaside Sitter era).

### Ideas for gravitational particle production

#### Cosmological Gravitational Particle Production (CGPP) through the Schrödinger Effect

Physica VI, no 9

October 1939

#### THE PROPER VIBRATIONS OF THE EXPANDING UNIVERSE

by ERWIN SCHRÖDINGER

§ 1. Introduction and summary. Wave mechanics imposes an a priori reason for assuming space to be closed; for then and only then are its proper modes discontinuous and provide an adequate description of the observed atomicity of matter and light. — Einsteins theory of gravitation imposes an a priori reason for assuming space to be, if closed, expanding or contracting; for this theory does not admit of a stable static solution. — The observed facts are, to say

900

ERWIN SCHRÖDINGER

These are the broad results. A finer and particularly interesting phenomenon is the following.

The decomposition of an arbitrary wave function into proper vibrations is rigorous, as far as the functions of space (amplitude-functions) are concerned, which, by the way, are exactly the same as in the static universe. But it is known, that, with the latter, two frequencies, equal but of opposite sign, belong to every space function. These two proper vibrations cannot be rigorously separated in the expanding universe. That means to say, that if in a certain moment only one of them is present, the other one can turn up in the course of time.

Generally speaking this is a phenomenon of outstanding importance. With particles it would mean production or anihilation of matter, merely by the expansion, whereas with light there would be a production of light travelling in the opposite direction, thus a sort of reflexion of light in homogeneous space. Alarmed by these prospects, I have investigated the question in more detail. Fortunately the equations admit of a solution by familiar functions, if R is a linear function of time. It turns out, that in this case the alarming

# The Schwinger Effect

Electric field ----- Particle creation

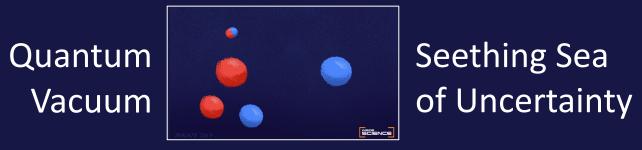


Image: Malate 2017 (AIP)

Turn on  $ec{E}$  field



Particle creation from the vacuum if energy gained in acceleration from  $ec{E}$  field over a Compton wavelength exceeds the particle's rest mass.

$$\left| \vec{E}_{\text{crit}} \right| = \frac{m_e^2 c^3}{e\hbar} \approx 10^{16} \,\text{V cm}^{-1} \Longrightarrow \Gamma \propto e^{-\left| \vec{E}_{\text{crit}} \right| / \left| \vec{E} \right|}$$

Sauter (1931); Heisenberg & Euler (1935); Weisskopf (1936); Schwinger (1951)

## The Schrödinger Effect

Expanding space —— Particle creation

Quantum Vacuum



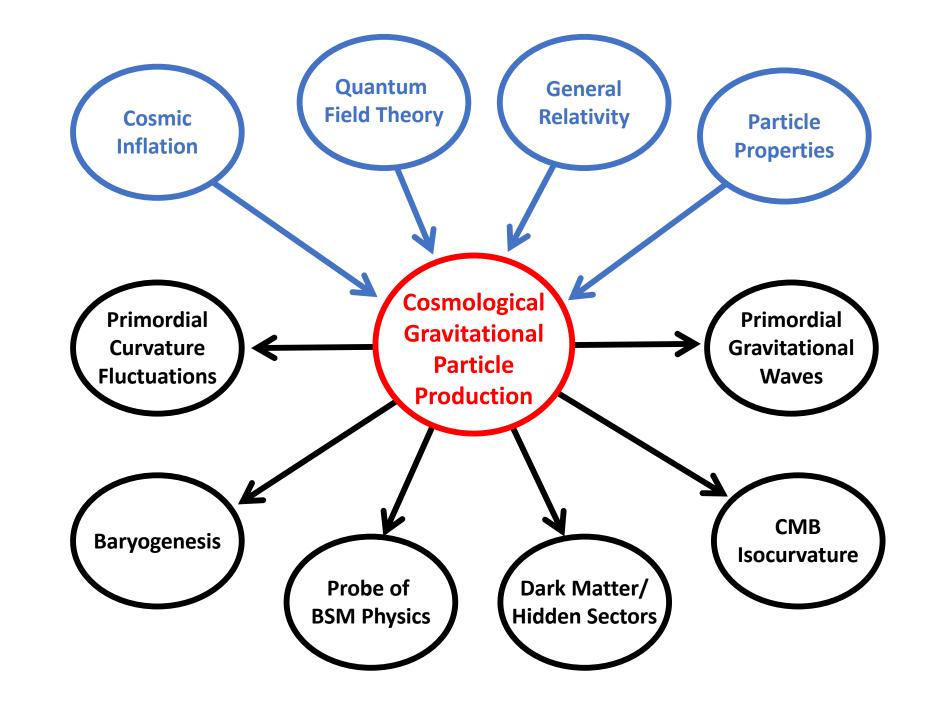
Image: Malate 2017 (AIP)

Turn on expansion



Particle creation from the vacuum if energy gained in acceleration from expansion over a Compton wavelength exceeds the particle's rest mass.

Hubble's law 
$$\, {\bf v} = Hd \,$$
  $\Longrightarrow \, H_{\rm crit} = m \, \Longrightarrow \, \Gamma \propto e^{-m/H} \,$  Schrödinger (1939)



### **Cosmological Gravitational Particle Production (CGPP)**

#### through the Schrödinger mechanism

Chung, EWK, Riotto (1998); Kuzmin & Tkachev (1999)

#### My collaborators:

Ivone Albuquerque Andrew Long

Edward Basso Evan McDonough

Christian Capanelli Guillaume Payeur

Tammi Chowdhury Toni Riotto

Daniel Chung Rachel Rosen

Patrick Crotty Leo Senatore

Michael Fedderke Alexei Starobinski

Gian Giudice Keyer Thyme

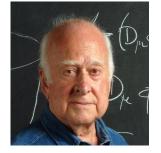
Lam Hui Igor Tkachev

Leah Jenks Jingyuan Wang

Siyang Ling Mark Wyman

Standard Model of Particle Physics





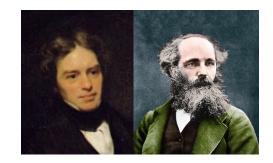
Higgs Boson

**Spin** 1/2



Leptons & Quarks

Spin 1



**Gauge Bosons** 

#### Standard Model of Particle Physics

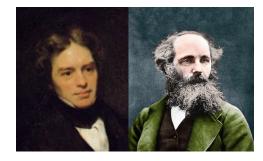


Spin 1





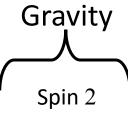
**Spin** 1/2

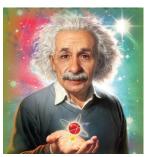


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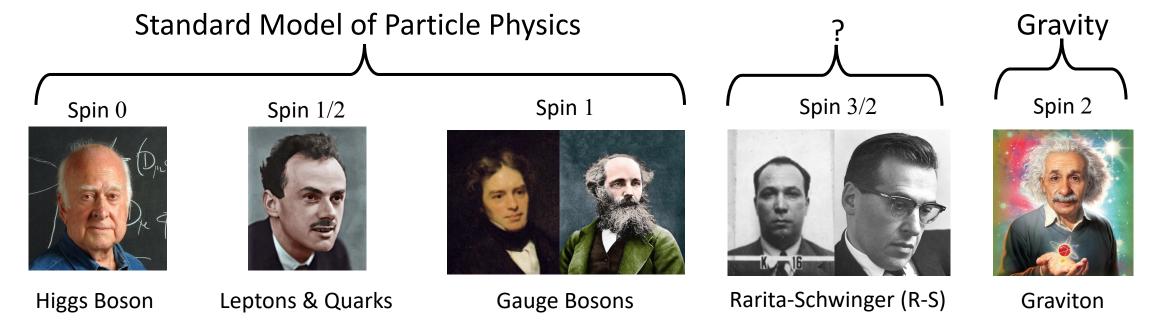
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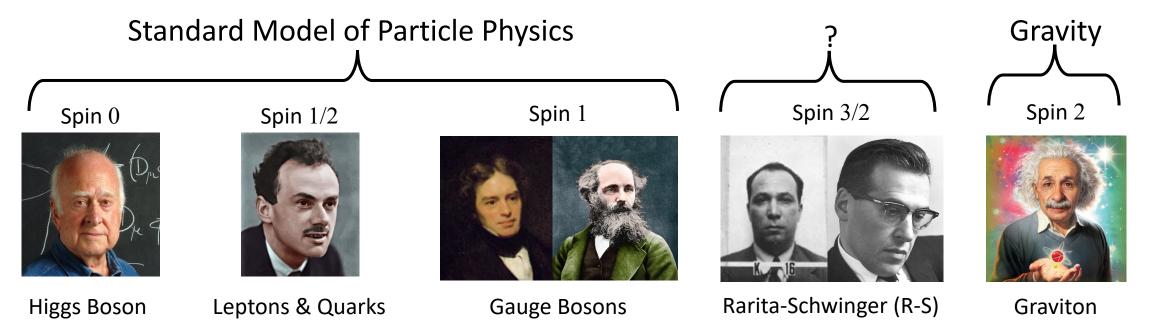
**Gauge Bosons** 



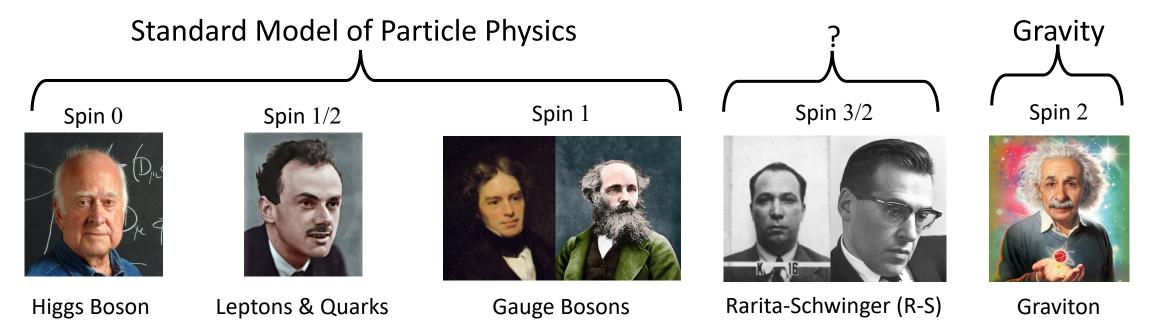


Graviton



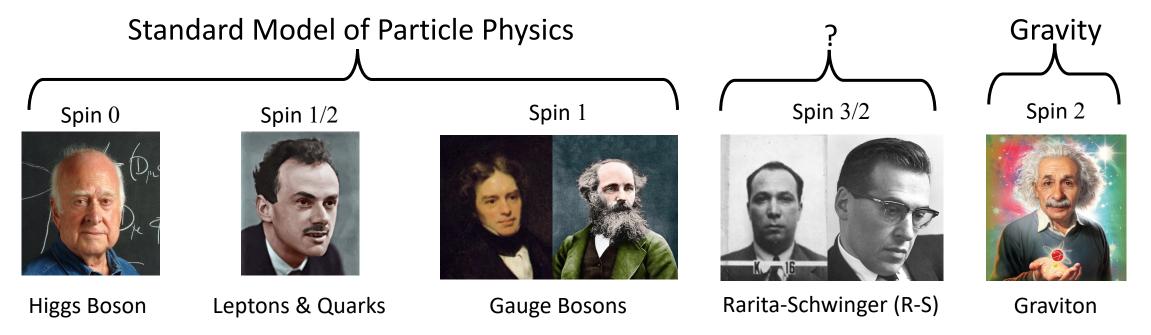


R-S fields do not appear in the standard model of particle physics, but are a legitimate subject as a quantum field theory.



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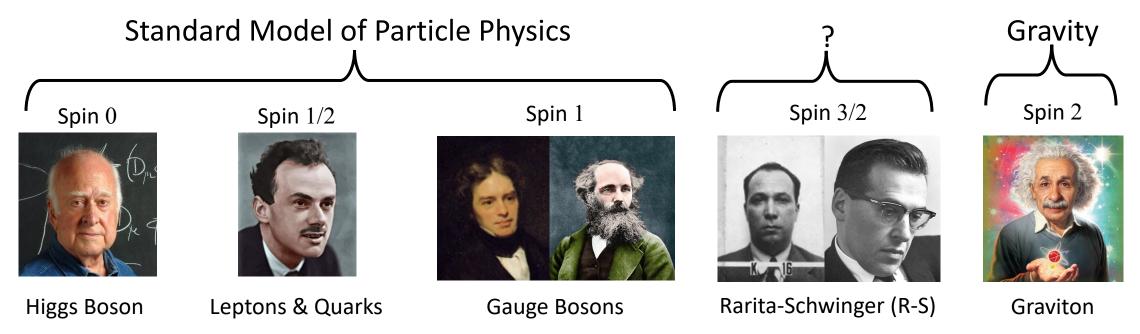
Massless R-S fields consistent only if coupled to a conserved current as in supersymmetry (Haag-Lopuszanski-Sohnius theorem).



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R-S field  $\Psi_{\mu}$  is a "vector-spinor" arising from the direct product of vector and Dirac spinor reps. of the Lorentz group.

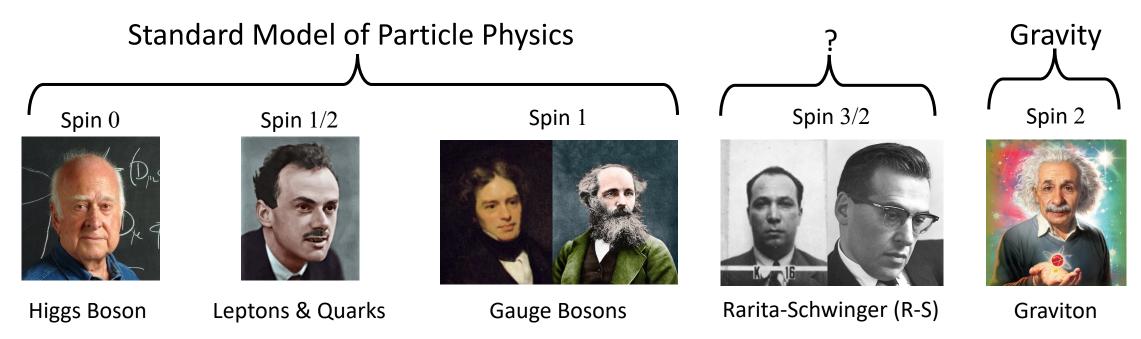


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$$\left(\frac{1}{2},\frac{1}{2}\right)\otimes\left[\left(\frac{1}{2},0\right)\oplus\left(0,\frac{1}{2}\right)\right]=\left(\frac{1}{2},1\right)\oplus\left(0,\frac{1}{2}\right)\oplus\left(1,\frac{1}{2}\right)\oplus\left(\frac{1}{2},0\right). \text{ Reducible representation } \left(\frac{1}{2},1\right)\oplus\left(1,\frac{1}{2}\right)=\text{RS field.}$$



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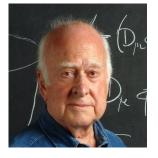
$$\left(\frac{1}{2},1\right)\oplus\left(1,\frac{1}{2}\right)$$
 can be decomposed into irreps. corresponding to  $\pm\frac{3}{2}$  and  $\pm\frac{1}{2}$  helicity states.

### Why study Rarita-Schwinger fields?

Standard Model of Particle Physics

Supergravity

 $\mathsf{Spin}\ 0$ 



Higgs Boson

**Spin** 1/2



Leptons & Quarks

Spin 1



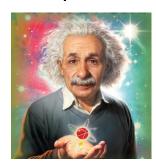
**Gauge Bosons** 

**Spin** 3/2



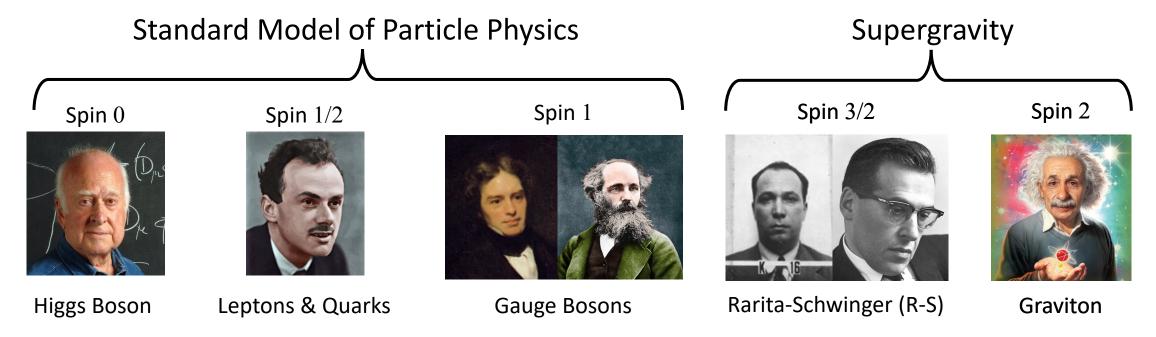
Rarita-Schwinger (R-S)

Spin 2



Graviton

### Why study Rarita-Schwinger fields?



In Supergravity (SUGRA), the spin 3/2 R-S field is the superpartner of the graviton, the *gravitino*.

Gravitino difficult to detect at LHC because of feeble gravitational coupling to SM fields, but ...

"Gravitino production leads to important constraints on early universe cosmology." (Supergravity, Freedman and Van Proeyen).

"Early universe cosmology (may) lead to important constraints on Supergravity model building." (EWK, Long, McDonough, PRD 2021 & PRL 2021; EWK, Long, McDonough, Wang 2025).

This is a work in progress with Andrew Long, Evan McDonough, and Jingyuan Wang.

### Why study CGPP of Rarita-Schwinger fields?

#### through the Schrödinger mechanism

I've studied CGPP of minimally-coupled scalars, conformally-coupled scalars, Dirac fermions, de Broglie-Proca fields, Kalb-Ramond fields, Fierz-Pauli fields, in one-field inflation models, rapid-turn inflation models, inflation models with non-canonical kinetic terms, Higgs-inflation models, ...

Aren't you tired of it? Don't you have anything better to do?

What could possibly be new with Rarita-Schwinger fields? Two answers:

- 1. possibility of vanishing sound speed,
- 2. in SUGRA models, generally RS field (the gravitino) has a dynamical mass.

Our (EWK, Long, McDonough, Wang) project goal is to calculate CGPP of gravitinos.

First step is to understand CGPP of "simple" R-S fields.

This is a progress report.

### Rarita-Schwinger field in FRW background

Covariant action for R-S field:  $\Psi_{\mu}=$  vector-spinor

Kallosh, Kofman, Linde, Van Proeyen (1999) Giudice, Riotto, Tkachev (1999)

 $S = \int d^4x \, e \left[ i \left( \frac{1}{4} \bar{\Psi}_{\mu} \, \underline{\gamma}^{\mu\nu\rho} \nabla_{\nu} \Psi_{\rho} - \frac{1}{4} \bar{\Psi}_{\mu} \overleftarrow{\nabla}_{\nu} \underline{\gamma}^{\mu\nu\rho} \Psi_{\rho} \right) - i \, \frac{1}{2} m \bar{\Psi}_{\mu} \gamma^{\mu\nu} \Psi_{\nu} \right]$ 

EWK, Long, McDonough (2021)

Specialize to FRW and define new field  $\psi_{\mu}(\eta,\vec{x})=a^{1/2}(\eta)\Psi_{\mu}(\eta,\vec{x})$  for canonical kinetic term

Impose constraints from field equations

Fourier decomposition 
$$\;\psi_{\mu}(\eta,\vec{x})=\int\!\!\frac{d^3\vec{k}}{(2\pi)^3}\,\psi_{\mu,\vec{k}}(\eta)\,e^{i\vec{k}\cdot\vec{x}}\;$$

Remove non-dynamical DOFs and decompose into helicity states:  $\psi_{\mu,\vec{k}} \longrightarrow \psi_{1/2,\vec{k}}$  and  $\psi_{3/2,\vec{k}}$ 

 $C_A$  and  $C_B$  are functions of  $H,\,R,\,m,\,\dot{m}$ 

### Rarita-Schwinger field in FRW background

Parameterize spinor wavefunctions in terms of helicity eigenspinors with mode functions

$$\chi_{A,3/2,\vec{k}}(\eta),\ \chi_{B,3/2,\vec{k}}(\eta),\ \chi_{A,1/2,\vec{k}}(\eta),\ \chi_{B,1/2,\vec{k}}(\eta)$$

Helicity-3/2 mode equation is just like Dirac field

Helicity-1/2 mode equation is more "interesting"

Eigenvalues of 1/2 mode equation are  $\pm \sqrt{|c_s|^2k^2+a^2m^2}$ 

$$|c_s|^2 = \frac{1}{9(H^2 + m^2)^2} \left[ \left( 3m^2 - \frac{1}{3}R - H^2 \right)^2 + 4\dot{m}^2 \right]$$

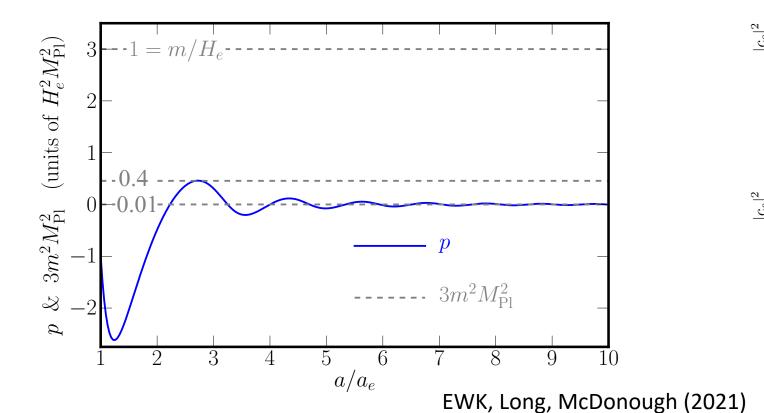
Vanishes for R-S fields, but can be nonzero for gravitinos

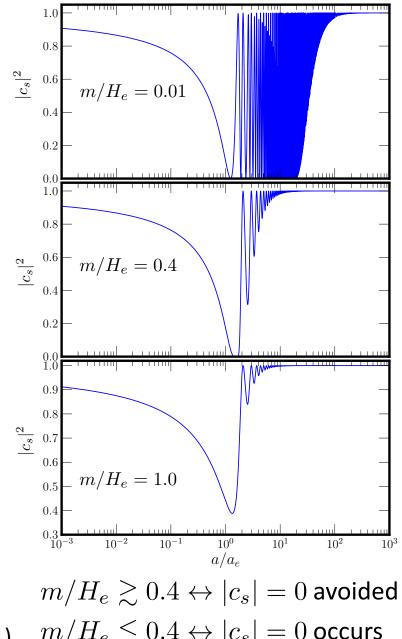
#### Sound speed can vanish

New feature (or is it a bug?): sound speed can vanish!

$$|c_s| = \frac{\left|3m^2 - \frac{1}{3}R - H^2\right|}{3m^2 + 3H^2} = \frac{\left|3m^2 - p/M_{\text{Pl}}^2\right|}{3m^2 + \rho/M_{\text{Pl}}^2}$$

$$|c_s|=1$$
 in dS ( $p=-
ho$ )  $|c_s|=0$  when  $p=3m^2M_{\rm Pl}^2$ 





 $m/H_e \lesssim 0.4 \leftrightarrow |c_s| = 0$  occurs

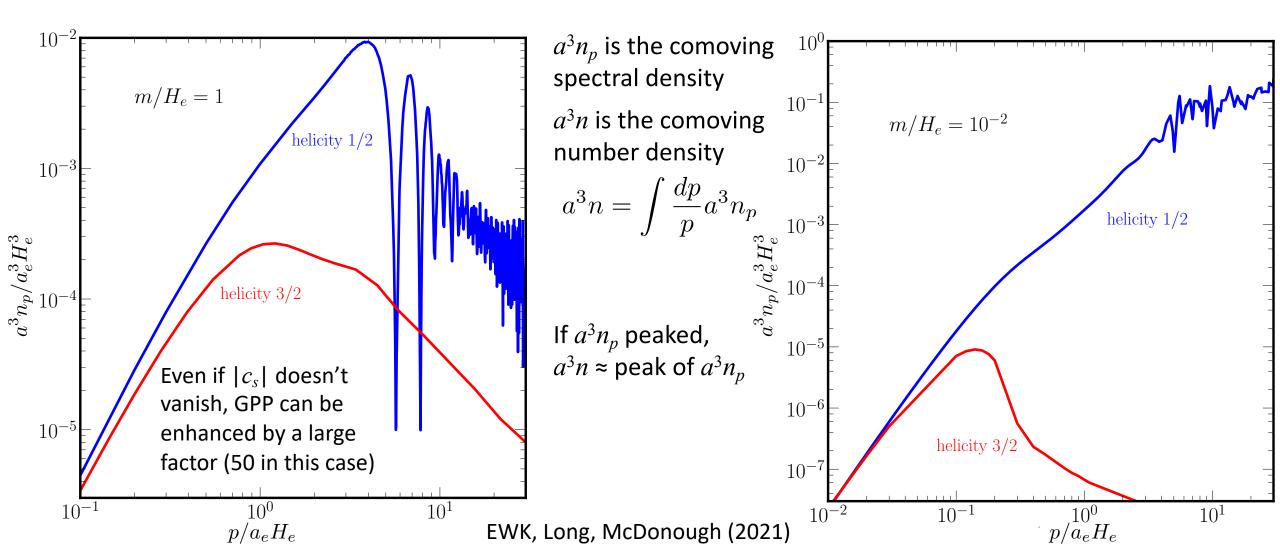
### Vanishing sound speed enhances GCPP

 $c_s$  varies for helicity-1/2 mode

$$\omega_k^2(\eta) = |c_s(\eta)|^2 k^2 + a^2(\eta) m^2$$

If  $|c_s| > 0$ ,  $\omega_k^2$  proportional to  $k^2$ , and CGPP suppressed for high-k modes

If  $|c_s| = 0$ ,  $\omega_k^2$  independent of  $k^2$ , and CGPP <u>unsuppressed</u> for high-k modes



### Vanishing sound speed enhances GCPP

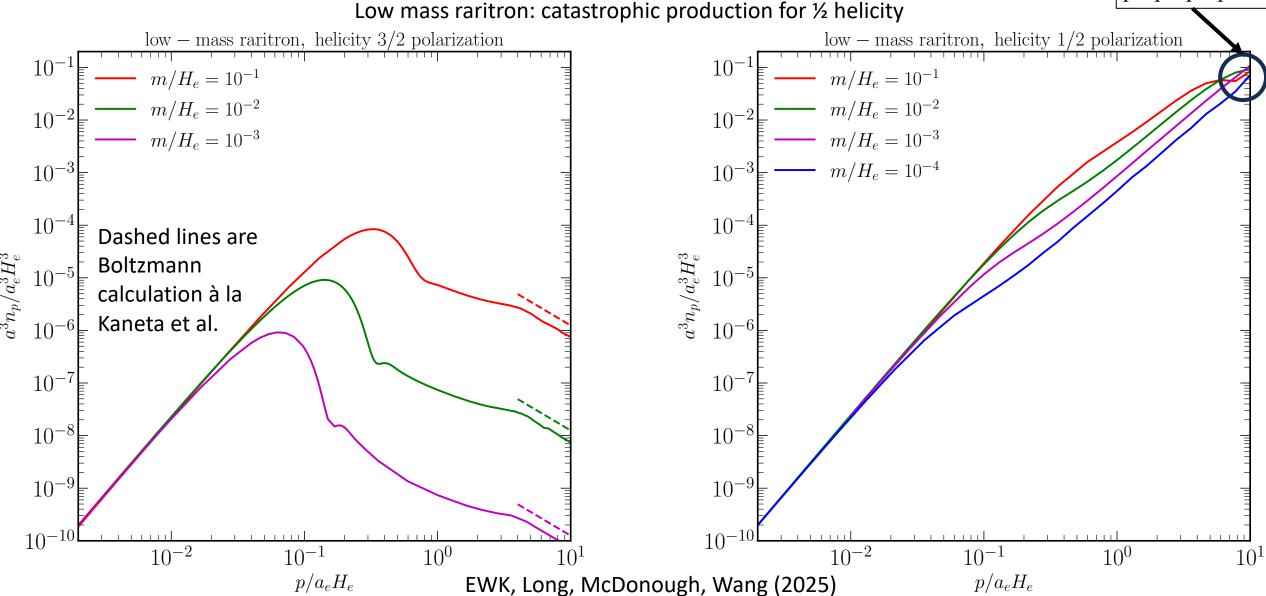
Call it a "raritron" (Kaneta, Ke, Mambrini, Olive, Verner 2023)

Unresolved

 $p^0, p^1, p^2, p^3$ ?

high-p

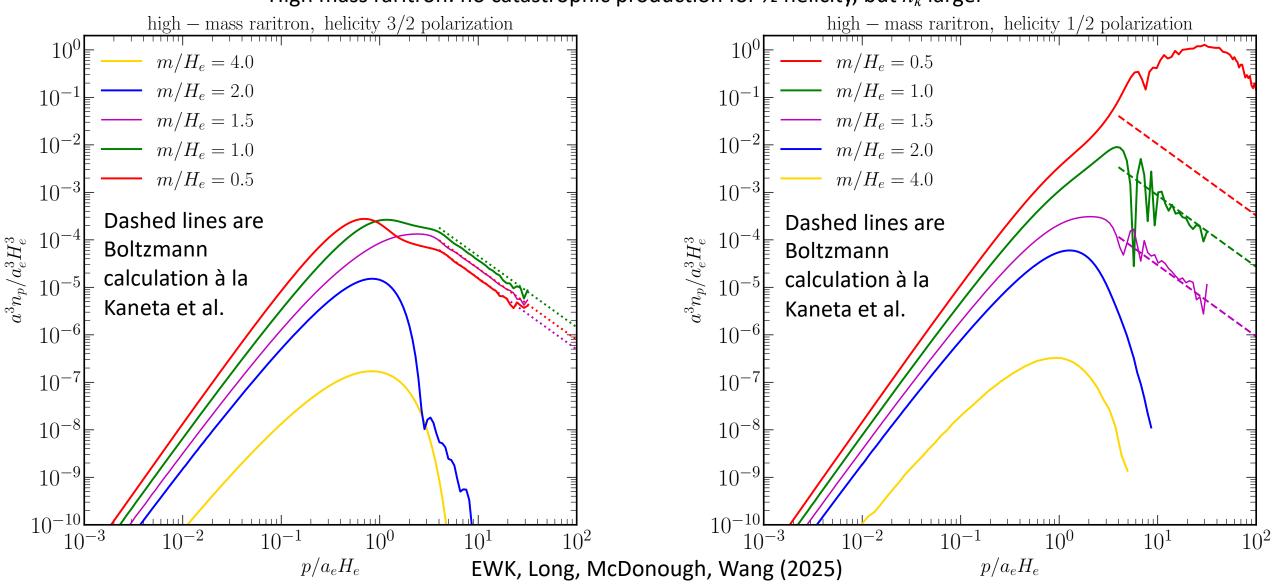
behavior



#### Vanishing sound speed enhances GCPP

Call it a "raritron" (Kaneta, Ke, Mambrini, Olive, Verner 2023)

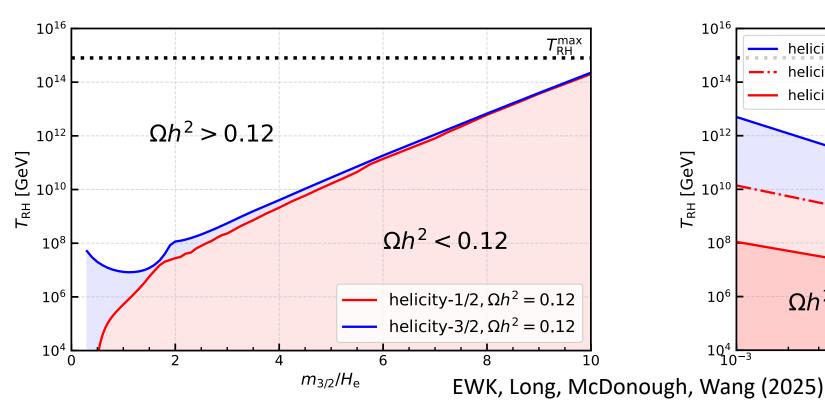
High mass raritron: no catastrophic production for  $\frac{1}{2}$  helicity, but  $n_k$  larger



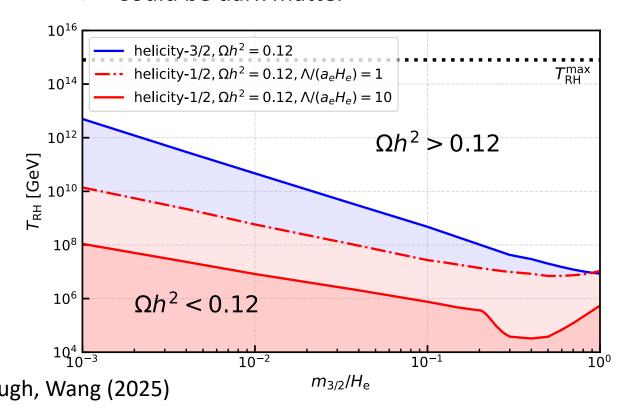
#### Rarita-Schwinger field can be dark matter

$$\boxed{\frac{\Omega h^2}{0.12} \approx \left(\frac{m}{H_e}\right) \left(\frac{H_e}{10^{12} \text{ GeV}}\right)^2 \left(\frac{T_{\text{RH}}}{10^9 \text{ GeV}}\right) \left(\frac{1}{10^{-5}} \cdot \frac{a^3 n}{a_e^3 H_e^3}\right)}$$

- For high-mass raritrons ( $m/H_e \gtrsim 0.4$ ):
  - $\blacktriangleright$  Helicity ½ dominates, esp. for  $m \lesssim 1.5 H_e$ .
  - $\triangleright$   $n_k$  decreases at large k, n and  $\Omega$  finite.
  - $\triangleright$  Could be dark matter for  $m \lesssim 10 H_e$ .

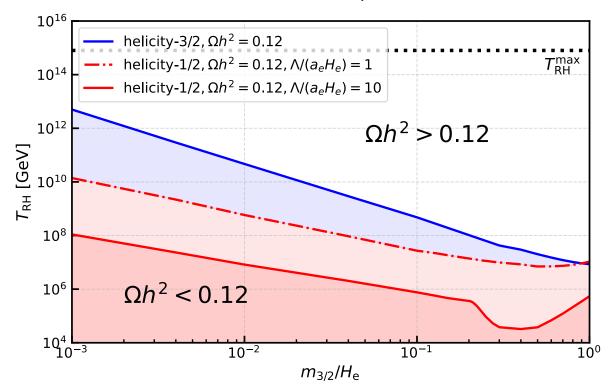


- For low-mass raritrons ( $m/H_e \lesssim 0.4$ ):
  - ➤ Helicity ½ dominates.
  - $\rightarrow$   $n_k$  unbounded at large k, so must either introduce cutoff, or have  $\dot{m} \neq 0$  (SUGRA?)
  - Could be dark matter



### Rarita-Schwinger field can be dark matter

- For low-mass raritrons  $(m_{3/2}/H_e \lesssim 0.1)$ :
  - For helicity 1/2,  $T_{\rm RH}$  scales as  $(m_{3/2}/H_e)^{-1}$  to obtain  $\Omega h^2 = 0.12$
  - For  $\Lambda/a_eH_e = 10$ , if  $T_{\rm RH} = 10^{15}\,{\rm GeV}$ ,  $\Omega h^2 = 0.12$  for  $m_{3/2}/H_e = 10^{-10}$
  - Can have very light raritron be dark matter
  - $\blacktriangleright$  If cutoff  $\Lambda > 10~a_eH_e$ , even lighter raritron possible for  $\Omega h^2 = 0.12$
  - > Similar conclusion in Kaneta et al., but different calculation



EWK, Long, McDonough, Wang (2025)

### **Varying R-S mass?**

#### Varying rarirton mass to remove catastrophic helicity ½ production

- Sound speed is complex,  $c_s = C_A + i C_B$
- Now just focus on  $|c_s|^2$  and consider  $|c_s|^2 = 1$

$$|c_s|^2 = \frac{1}{9(H^2 + m^2)^2} \left[ \left( 3m^2 - \frac{1}{3}R - H^2 \right)^2 + 4\dot{m}^2 \right]$$

$$|c_s(N)|^2 = 1 \Rightarrow \left(\frac{dm}{dN}\right)^2 = H^2 \left[1 + \frac{R}{12H^2}\right] \left[2 - \frac{R}{3H^2} + 6\frac{m^2}{H^2}\right] \qquad R = \text{Ricci scalar}$$

$$N = \ln(a/a_e)$$

$$dm \qquad \left[ \dot{\phi}^2 \right]^{1/2} \left[ V(\phi) \right] \qquad m^2 \, e^{1/2}$$

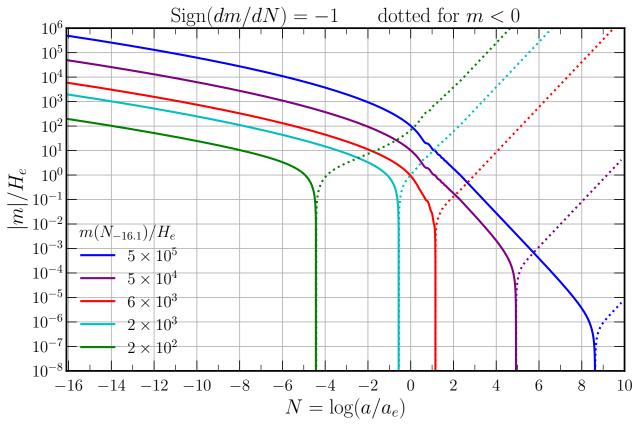
$$\frac{dm}{dN} = \pm H \left[\frac{\dot{\phi}^2}{2M_{\rm Pl}^2H^2}\right]^{1/2} \left[\frac{V(\phi)}{M_{\rm Pl}^2H^2} + 3\frac{m^2}{H^2}\right]^{1/2}$$
 Ambiguity in choice of sign.

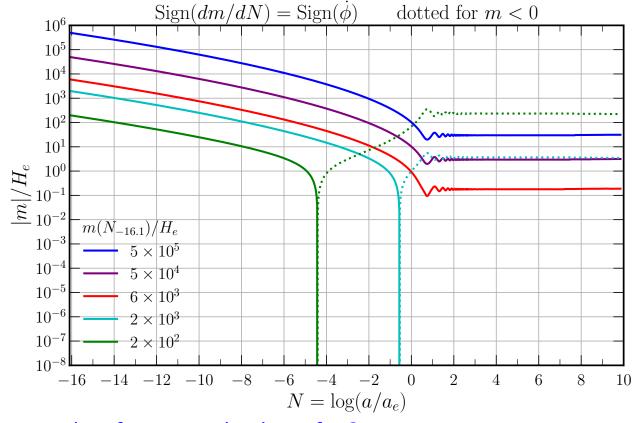
When dm/dN = 0, can change sign.

dm/dN = 0 when  $\dot{\phi} = 0$  or when m = 0 and  $V(\phi) = 0$ .

### **Varying R-S mass?**

 $|c_s|=1$  to remove catastrophic helicity ½ production? Require  $\dot{m}\neq 0$ . BUT WHY?





#### What fixes initial value of m?

 $m \to \infty$  at late time. Not acceptable.

Note: for fermion sign of *m* doesn't matter.

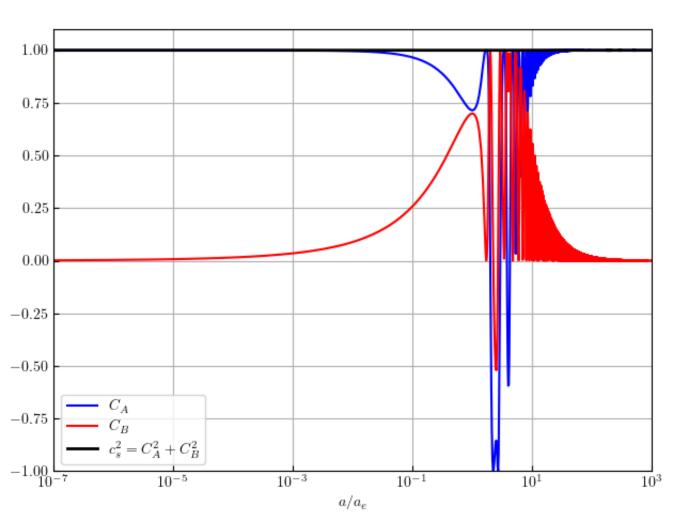
#### What fixes initial value of m?

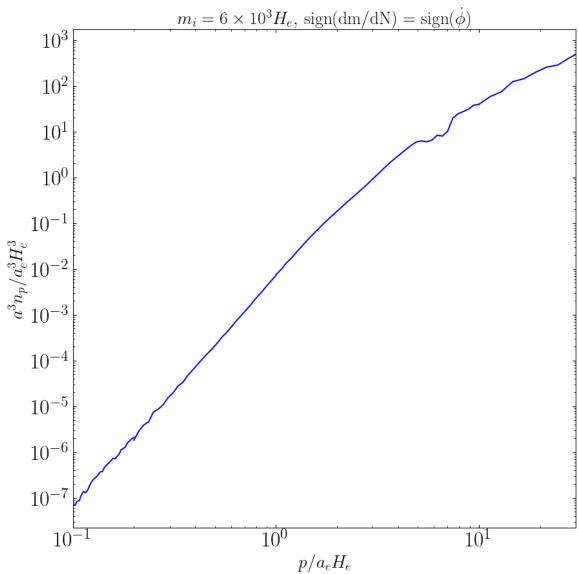
Sign of dm/dN changes every time  $\phi$  goes through 0. Nice m behavior at late time, but WHY change sign?

#### Answers must lie with Supergravity

### **Varying R-S mass?**

- Even with  $|c_s|^2 = 1$ , can still have catastrophic production.
- Sound speed is complex:  $c_s = C_A + i C_B$ .
- It can be pure imaginary when  $C_A = 0$ !





### **Gravitino in FRW background**

Spin-3/2 particles arise in theories of supergravity; s = 3/2 gravitino is superpartner of s = 2 graviton

Does supergravity have a catastropic production of gravitinos? It depends on the model!

For models with a single chiral superfield  $\Phi$  with Kahler potential  $K(\Phi,\bar\Phi)=\Phi\bar\Phi$ , superpotential  $W(\Phi)=rac12 m_\phi\Phi^2$ 

$$m_{3/2} = e^{K(\Phi,\bar{\Phi})/2M_{\rm Pl}^2} \frac{W(\Phi)}{M_{\rm Pl}^2} = e^{\phi^2/4M_{\rm Pl}^2} \frac{m_\phi}{4M_{\rm Pl}^2} \phi^2$$

$$V(\phi) = \frac{1}{2} m_{\phi}^2 \phi^2 \ e^{\phi^2 / 2M_{\text{Pl}}^2} \left( 1 + \frac{\phi^2}{8M_{\text{Pl}}^2} + \frac{\phi^4}{16M_{\text{Pl}}^2} \right)$$

$$\dot{m}_{3/2} = \text{Sign}(\phi\dot{\phi}) \left[\frac{\dot{\phi}^2}{2M_{\text{Pl}}^2}\right]^{1/2} \left[\frac{V(\phi)}{M_{\text{Pl}}^2} + 3m_{3/2}^2\right]^{1/2}$$

Time-dependent gravitino mass (depends on rolling inflaton)  $\Rightarrow |c_s| = 1$  at all times & no catastrophic production. But issues:

- 1. SUSY restored at late times when  $\phi = 0$
- 2. model doesn't inflate

#### **Gravitino in FRW background**

For models with two chiral superfields

 $|c_s|$  depends on relative orientation of inflaton direction & SUSY breaking direction

 $|c_s|=0$  occurs in models with a nilpotent superfield  $S^2=0$  and orthogonal constraint  $S\cdot (\Phi-ar\Phi)=0$ 

EWK, Long, McDonough (2021)  $\times$  2

#### But even more complications:

why not three chiral superfields gravitino may mix with inflation mixing between the goldstino & inflatino can avoid the catastrophe (explicit calculation needed) many other fields vanishing sound speed may not be catastrophic

Dudas, Garcia, Mambrini, Olive, Peloso, Verner (2021)
Antoniadis, Benaki, Ke (2021)

# **Rarita-Schwinger Fields and Cosmology**

- Preliminary results!
- It's still a work in progress (things take longer than they do).
- What we (EWK, Long, McDonough, Wang) plan to accomplish in the first paper:
  - Convincingly demonstrate (again) that Boltzmann approach is not the compete picture.
  - Calculate relic density for R-S fields, including possibility of zero sound speed. (Kaneta, Ke, Mambrini, Olive, Verner (2023) ignored zero sound speed and only considered Boltzmann)
    - If constant mass RS, must employ cutoff for low masses.
  - Explore parameter space for R-S field (raritron) to be dark matter.
  - $\triangleright$  Explore possibilities for an R-S field for varying m.
- In a subsequent paper we will consider CGPP of gravitino, inflatino, goldstino, (s)goldstino, whateverino in several Supergravity models.



My experience with Supergravity

https://youtu.be/ozA0VmIsCNs?feature=shared

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