GW probes of physics beyond the standard model 4

SGWB GENERATED BY SUPERCONDUCTING COSMIC STRINGS

Based on: I. Yu. Rybak & L. Sousa, JCAP 11 (2022) 024 (arXiv: 2209.01068) I. Yu. Rybak & L. Sousa, Phys.Rev.D 111 (2025) 8, 083502 (arXiv: 2412.17154)

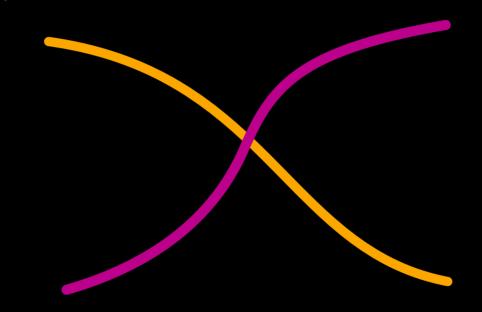


Institute of Astrophysics and Space Sciences

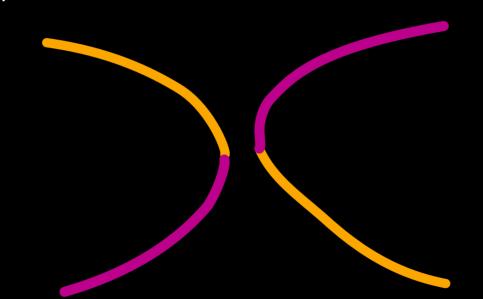
www.iastro.pt

LARA SOUSA Lara.Sousa@astro.up.pt

Upon collision

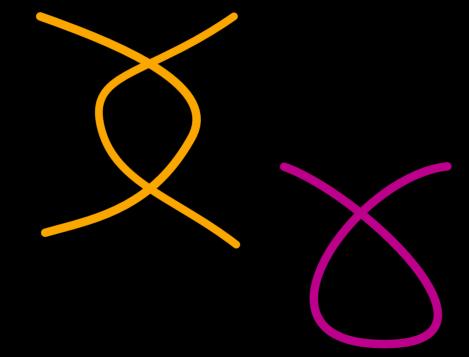


Upon collision



Strings exchange partners and intercommute.

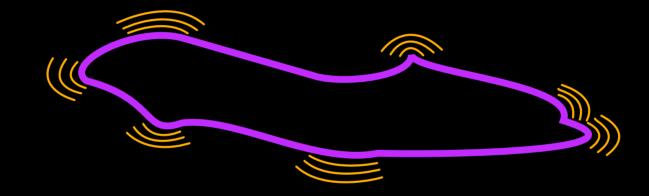
Some situations...



Some situations...

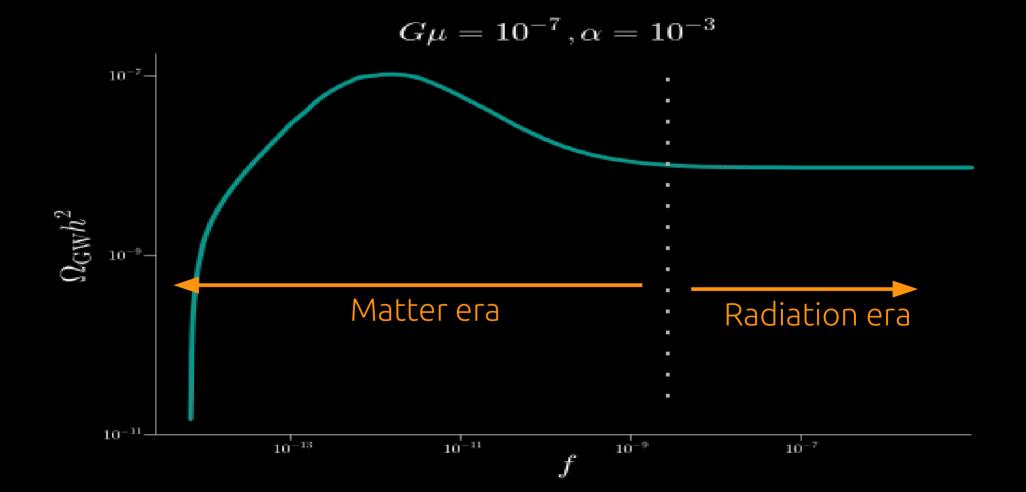
lead to the copious production of cosmic string loops!

Loops detach form the network and start to oscilate



and generate transient gravitational wave bursts.

THE TYPICAL COSMIC STRING SGWB



LOOPS AND GRAVITATIONAL WAVES

TO COMPUTE THE SGWB GENERATED BY COSMIC STRINGS WE NEED TO KNOW THE NUMBER DENSITY OF LOOPS $n(\ell(t), t)$

How many loops are created?

How much of the energy of the loops goes into GWs? What is the emission spectrum of loops?

In many GUTs, cosmic strings may carry currents and behave as thin superconductor wires (Witten 1985).

Spontaneous current generation may happen even in the standard GUT paradigm (Davis and Peter, 1995).

In many GUTs, cosmic strings may carry currents and behave as thin superconductor wires (Witten 1985).

Spontaneous current generation may happen even in the standard GUT paradigm (Davis and Peter, 1995).

REALISTIC COSMIC STRINGS MAY BE CURRENT-CURRYING AND THUS HAVE INTERNAL DEGREES OF FREEDOM

SUPERCONDUCTING STRINGS BEHAVE AS **ELASTIC STRINGS** which have a distinct tension and energy per unit length

There are two types of perturbations: * Wiggles: wordsheet displacements * Woggles: longitudinal displacements

SUPERCONDUCTING STRINGS BEHAVE AS ELASTIC STRINGS which have a distinct tension and energy per unit length

There are two types of perturbations: * Wiggles: wordsheet displacements * Woggles: longitudinal displacements

We use **TRANSONIC ELASTIC STRINGS**, for which the speed of propagation of wiggles and woggles are equal, as a proxy to study the gravitational wave background generated by superconducting strings

TRANSONIC STRING LOOPS

$$X^{\mu} = \frac{T_{\ell}}{2\pi} \left[X^{\mu}_{+} \left(\sigma_{+} \right) + X^{\mu}_{-} \left(\sigma_{-} \right) \right],$$

$$\phi = \frac{T_{\ell}}{2\pi} \left[F_{+} \left(\sigma_{+} \right) + F_{-} \left(\sigma_{-} \right) \right] \,,$$

with

$$\mathbf{X}_{+}^{\prime 2}(\sigma_{+}) = 1 - F_{+}^{\prime 2}(\sigma_{+}), \quad \mathbf{X}_{-}^{\prime 2}(\sigma_{-}) = 1 - F_{-}^{\prime 2}(\sigma_{-})$$

LOOPS AND GRAVITATIONAL WAVES

TO COMPUTE THE SGWB GENERATED BY COSMIC STRINGS WE NEED TO KNOW THE NUMBER DENSITY OF LOOPS $n(\ell(t), t)$

How many loops are created?

How much of the energy of the loops goes into GWs? What is the emission spectrum of loops?

GW EMISSION EMISSION EFFICIENCY

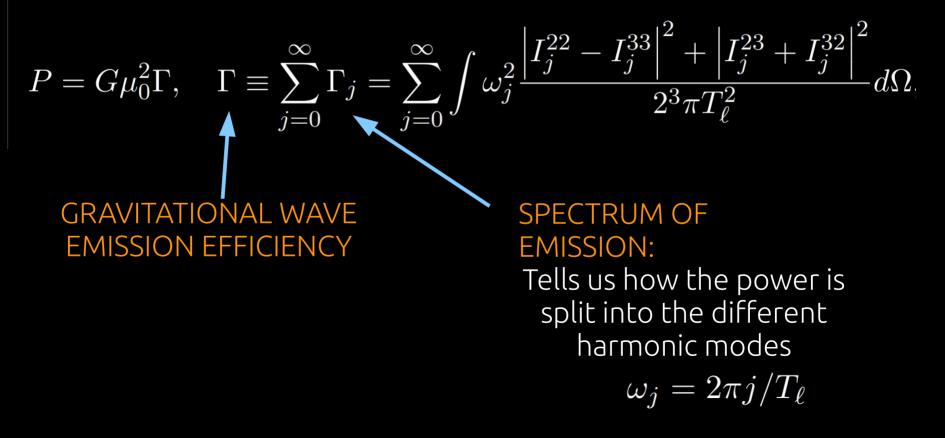
Power emitted in GWs:

$$P = G\mu_0^2 \Gamma, \quad \Gamma \equiv \sum_{j=0}^{\infty} \Gamma_j = \sum_{j=0}^{\infty} \int \omega_j^2 \frac{\left|I_j^{22} - I_j^{33}\right|^2 + \left|I_j^{23} + I_j^{32}\right|^2}{2^3 \pi T_\ell^2} d\Omega,$$

GRAVITATIONAL WAVE
EMISSION EFFICIENCY

GW EMISSION EMISSION EFFICIENCY

Power emitted in GWs:



GW EMISSION EMISSION EFFICIENCY

Power emitted in GWs:

$$P = G\mu_0^2 \Gamma, \quad \Gamma \equiv \sum_{j=0}^{\infty} \Gamma_j = \sum_{j=0}^{\infty} \int \omega_j^2 \frac{\left|I_j^{22} - I_j^{33}\right|^2 + \left|I_j^{23} + I_j^{32}\right|^2}{2^3 \pi T_\ell^2} d\Omega_j$$

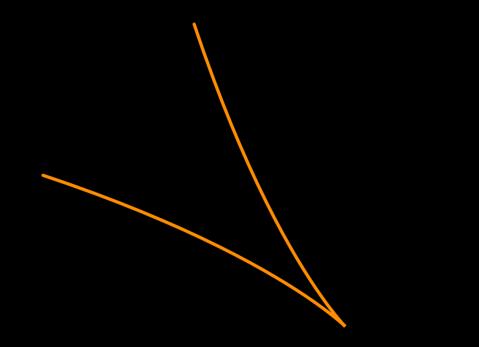
with

$$I_{\pm}^{\mu} = \frac{T_{\ell}}{\pi} \int_{0}^{2\pi} X_{\pm}^{\prime \mu} e^{-\frac{iT_{\ell}}{2\pi}k_{\nu}X_{\pm}^{\nu}} d\sigma_{\pm}$$

$$\tilde{T}^{\mu\nu}(\omega, \mathbf{k}) = \frac{1}{T_{\ell}} \int T^{\mu\nu} \mathrm{e}^{-ik_{\nu}X^{\nu}} d^{4}x = \frac{\mu_{0}}{2T_{\ell}} I^{(\mu}_{+}I^{\nu)}_{-}$$

EMISSION FROM A CUSP-LIKE POINT

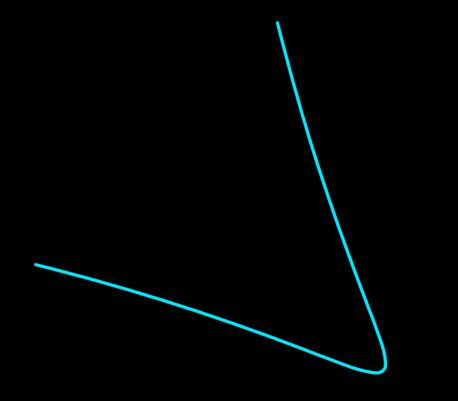
At some points on string loops, known as CUSPS, string velocity can equal the speed of light.



CUSPS EMIT HIGHLY BEAMED GRAVITATIONAL WAVE BURSTS

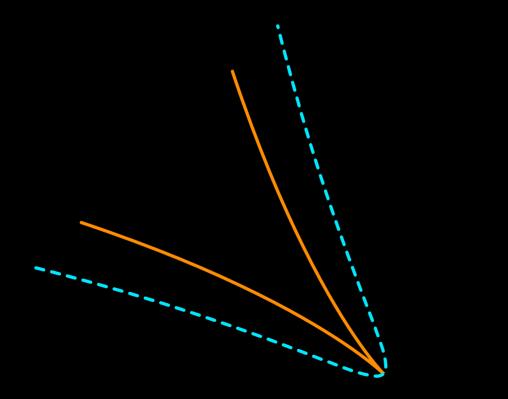
EMISSION FROM A CUSP-LIKE POINT

For current-carrying strings, CUSPS CAN NO LONGER FORM.



EMISSION FROM A CUSP-LIKE POINT

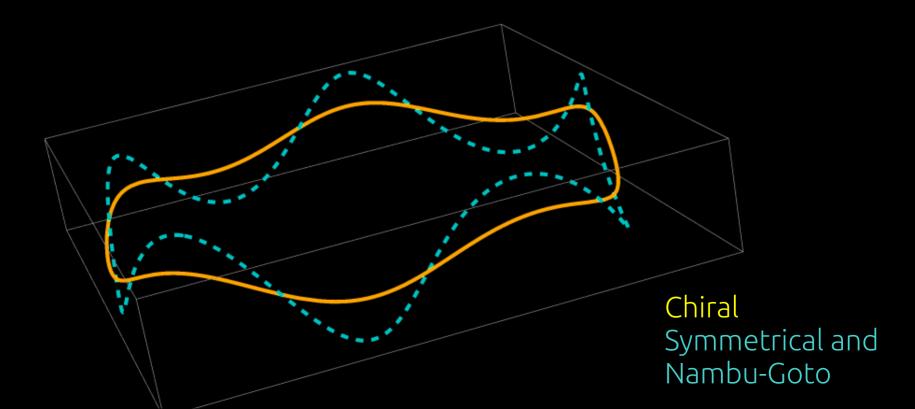
For current-carrying strings, CUSPS CAN NO LONGER FORM.



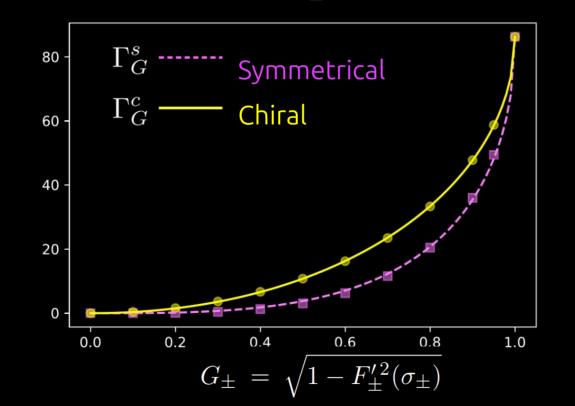
IF CURRENT IS SYMMETRICAL, HOWEVER, CUSP-LIKE POINTS MAY FORM, BUT NOW THEIR VELOCITY IS SUBLUMINAL

EMISSION FROM BURDEN LOOPS

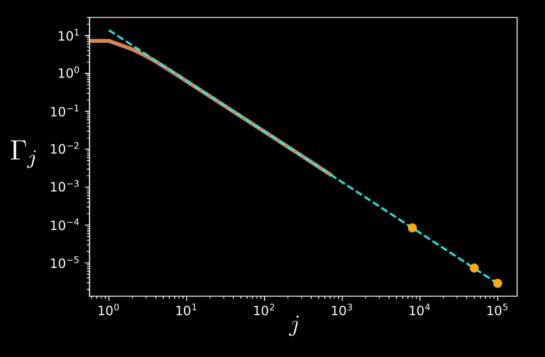
Burden Loops create cusps (or cusp-like points) at discrete instants of time



Gravitational wave emission efficiency decreases with increasing current



THE PRESENCE OF CURRENT LEADS TO A SUPPRESSION OF THE EMISSION OF GRAVITATIONAL RADIATION

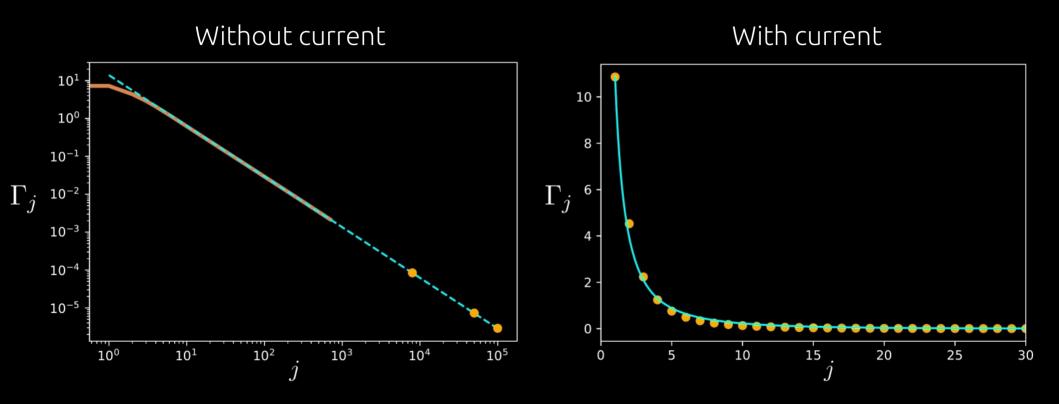


Without current, we have a power law spectrum

$$\Gamma_j \sim j^{-q}$$

For large enough j.

(Vaschaspati & Vilenkin, 1985)

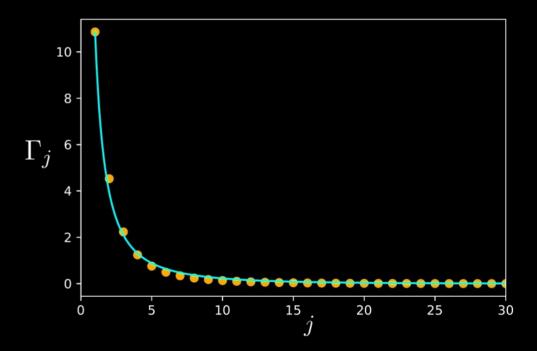


With current, we have an exponential decay

$$\Gamma_j \sim j^{-q} \mathrm{e}^{-j f_m(G_{\pm})}$$

with

$$f_m(G_{\pm}) = a_m (1 - \sqrt{G_{\pm}})^{b_m}$$



THE POWER EMITTED IN GWS BY A LOOP WITH QUASI-CUSPS DECAYS EXPONENTIALLY WITH INCREASING HARMONIC MODE FOR NULL AND SYMMETRICAL CURRENTS

EMISSION FROM A KINK

String collisions and intercommutation give rise to discontinuities in the string tangent, known as KINKS.

For Nambu-Goto strings, kinks travel along the string at the speed of light.

KINKS EMIT "FAN-LIKE" GRAVITATIONAL WAVE BURSTS

EMISSION FROM A KINK

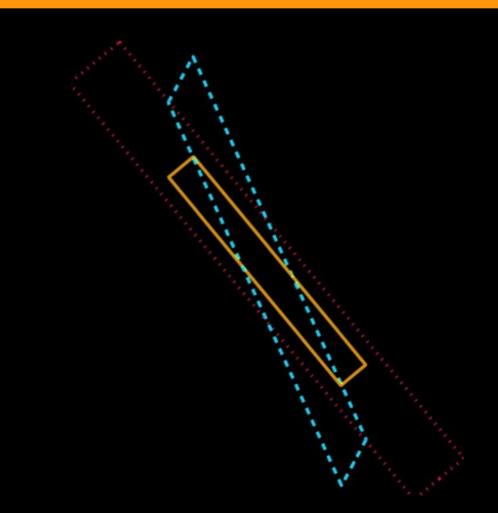
String collisions and intercommutation give rise to discontinuities in the string tangent, known as KINKS.

If there is current traveling along the string, kinks are necessarily slower GRAVITATIONAL WAVE BURST FROM KINKS ON SUPERCONDUCTING STRINGS ARE WEAKER

EMISSION FROM CUSPLESS LOOPS

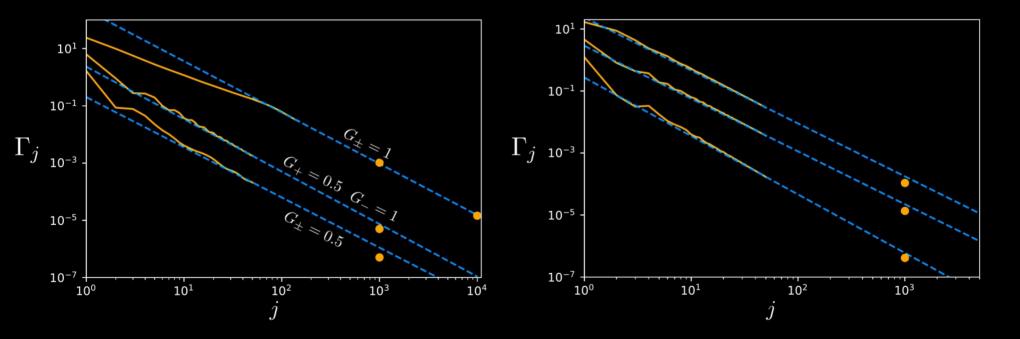
Loops that are Piece-wise straight And have no cusps

> Chiral Symmetrical Nambu-Goto



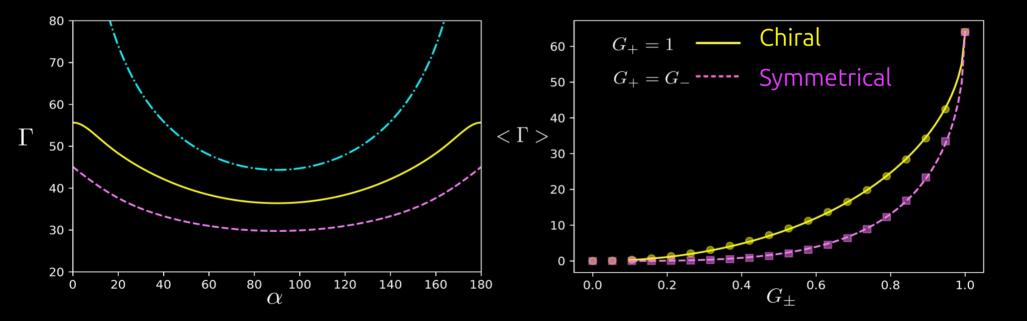
EMISSION FROM CUSPLESS LOOPS

In this case, the spectrum of emission is not affected by the inclusion of current: it is still a power law



EMISSION FROM CUSPLESS LOOPS

The gravitational wave efficiency, however, is affected precisely in the same way as before



IMPACT OF CURRENT ON GW EFFICIENCY

GRAVITATIONAL WAVE EMISSION EFFICIENCY FOR CURRENT-CARRYING STRINGS IS GIVEN BY

$$\Gamma_G^m = \Gamma_0 (1 - |F'_{\pm}|)^{B_{\Gamma}^m}$$

Where, for symmetrical currents,

 $B_\Gamma^spprox 2$ For loops with cusps $B_\Gamma^spprox 1.5$ For loops with kinks

And $B_{\Gamma}^{s} \approx \sqrt{2}B_{\Gamma}^{c}$ for chiral superconducting loops.

LOOPS AND GRAVITATIONAL WAVES

TO COMPUTE THE SGWB GENERATED BY COSMIC STRINGS WE NEED TO KNOW THE NUMBER DENSITY OF LOOPS $n(\ell(t), t)$

How many loops are created?

How much of the energy of the loops goes into GWs? What is the emission spectrum of <u>loops?</u>

LOOPS AND VECTOR RADIATION

Power emitted in Vector radiation:

$$P = \sum_{j} P_{j} = e^{2} \Gamma^{\text{em}},$$
VECTOR RADIATION
EMISSION EFFICIENCY

$$\frac{dP_{j}}{d\Omega} = -\frac{\omega_{j}^{2}}{2\pi} j^{\mu} j_{\mu}^{*} = e^{2} \frac{d\Gamma^{\text{em}}}{d\Omega}$$
SPECTRUM OF
EMISSION:
Tells us how the power is
split into the different
harmonic modes

LOOPS AND VECTOR RADIATION

Power emitted in Vector radiation:

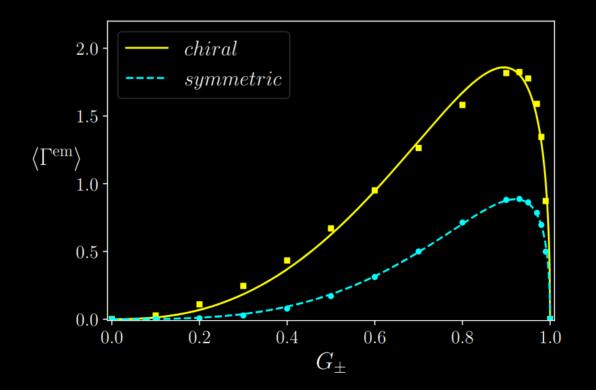
$$P = \sum_{j} P_{j} = e^{2} \Gamma^{\text{em}}, \qquad \frac{dP_{j}}{d\Omega} = -\frac{\omega_{j}^{2}}{2\pi} j^{\mu} j_{\mu}^{*} = e^{2} \frac{d\Gamma^{\text{em}}}{d\Omega}$$

with

$$j^{\mu} = e \frac{L}{8\pi^{2}} \left(I_{-} J_{+}^{\mu} - I_{+} J_{-}^{\mu} \right),$$
$$I_{\pm} = \int_{0}^{2\pi} F_{\pm}' e^{ij\left(\sigma_{\pm} - \frac{2\pi}{L} \mathbf{n} \cdot \mathbf{X}_{\pm}\right)} d\sigma_{\pm},$$
$$J_{\pm}^{\mu} = \int_{0}^{2\pi} X_{\pm}'^{\mu} e^{ij\left(\sigma_{\pm} - \frac{2\pi}{L} \mathbf{n} \cdot \mathbf{X}_{\pm}\right)} d\sigma_{\pm}.$$

LOOPS AND VECTOR RADIATION

Vector radiation emission efficiency also decreases with increasing current, but is also suppressed for very low currents



LOOPS AND VECTOR RADIATION

VECTOR RADIATION EMISSION EFFICIENCY FOR CURRENT-CARRYING STRINGS IS GIVEN BY

$$\langle \Gamma^{\mathrm{em}} \rangle = \Gamma_0^{\mathrm{em}} \left| F_{\pm}' \right| \left(1 - \left| F_{\pm}' \right| \right)^D$$

With

	$\Gamma_0^{\rm em}$	D
Symmetric loop with quasi-cusps	4.9	1.6
Symmetric loop with kinks	10.5	1.8
Chiral loop with quasi-cusps	8.6	1.1
Chiral loop with kinks	8.6	1.2

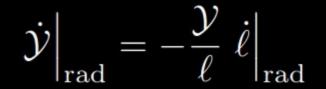
Loop length:

$$\dot{\ell} = -G\mu_0\Gamma^{\rm gr}(\mathcal{Y}) - \tilde{e}^2\Gamma^{\rm em}(\mathcal{Y}),$$

Loop length:

$$\dot{\ell} = -G\mu_0\Gamma^{\rm gr}(\mathcal{Y}) - \tilde{e}^2\Gamma^{\rm em}(\mathcal{Y}),$$

Current:



Loop length:

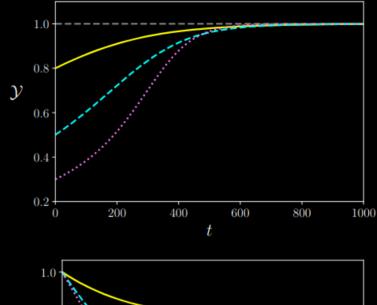
$$\dot{\ell} = -G\mu_0\Gamma^{\rm gr}(\mathcal{Y}) - \tilde{e}^2\Gamma^{\rm em}(\mathcal{Y}),$$

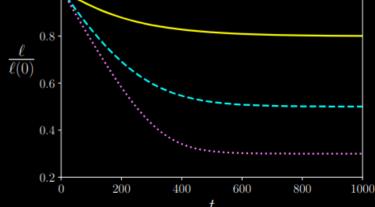
Current:

$$\dot{\mathcal{Y}} = \frac{\mathcal{Y}}{\ell} \left[G\mu_0 \Gamma^{\mathrm{gr}}(\mathcal{Y}) + \tilde{e}^2 \Gamma^{\mathrm{em}}(\mathcal{Y}) - A(\mathcal{Y}) \right]$$
Charge leakage

In the absence of charge leakage, VORTONS FORM

NO SIGNIFICANT GW EMISSION IS EXPECTED

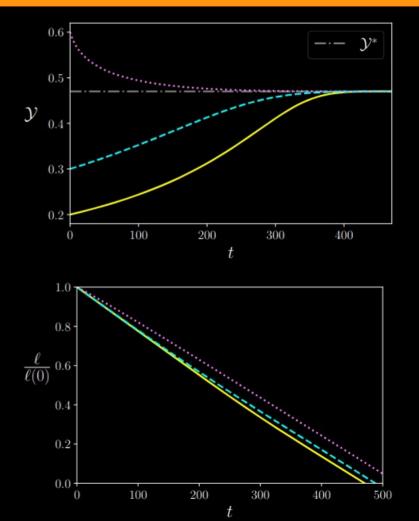




But in the presence of charge leakage, A SCALING SOLUTION EMERGES:

$$\dot{\ell} = \text{constant} \quad \text{and} \quad \dot{\mathcal{Y}} = 0$$

$$G\mu_0\Gamma^{\mathrm{gr}}(\mathcal{Y}^*) + \tilde{e}^2\Gamma^{\mathrm{em}}(\mathcal{Y}^*) = A(\mathcal{Y}^*)$$



WE MAY HAVE A SIGNIFICANT SGWB FROM SUPERCONDUCTING LOOPS WITH CONSTANT CURRENT

LOOPS AND GRAVITATIONAL WAVES

TO COMPUTE THE SGWB GENERATED BY COSMIC STRINGS WE NEED TO KNOW THE NUMBER DENSITY OF LOOPS $n(\ell(t), t)$

How many loops are created?

How much of the energy of the loops goes into GWs? What is the emission spectrum of <u>loops</u>?

(SEMI-)ANALYTICAL APPROACH

Sousa & Avelino 2013 (arXiv: 1304.2445); Sousa, Avelino & Guedes 2020 (arXiv: 2002.01709)

PREMISE: the large-scale evolution of the string network determines how much energy goes into loops:

$$\dot{\rho}_{\ell} = \left. \frac{d\rho}{dt} \right|_{loops} = \tilde{c}v\frac{\rho}{L} \sim \frac{v}{L^3}$$

(SEMI-) ANALYTICAL APPROACH

Sousa & Avelino 2013 (arXiv: 1304.2445); Sousa, Avelino & Guedes 2020 (arXiv: 2002.01709)

PREMISE: the large-scale evolution of the string network determines how much energy goes into loops:

$$\dot{\rho}_{\ell} = \left. \frac{d\rho}{dt} \right|_{loops} = \tilde{c}v\frac{\rho}{L} \sim \frac{v}{L^3}$$

ASSUMPTION: Loops are created with a length that is a fixed fraction of the characteristic length $\ell = \alpha L$

(SEMI-)ANALYTICAL APPROACH

Sousa & Avelino 2013 (arXiv: 1304.2445); Sousa, Avelino & Guedes 2020 (arXiv: 2002.01709)

PREMISE: the large-scale evolution of the string network determines how much energy goes into loops:

$$\dot{\rho}_{\ell} = \left. \frac{d\rho}{dt} \right|_{loops} = \tilde{c}v\frac{\rho}{L} \sim \frac{v}{L^3}$$

ASSUMPTION: Loops are created with a length that is a fixed fraction of the characteristic length $\ell=\alpha L$

NUMBER DENSITY OF LOOPS PRODUCED:

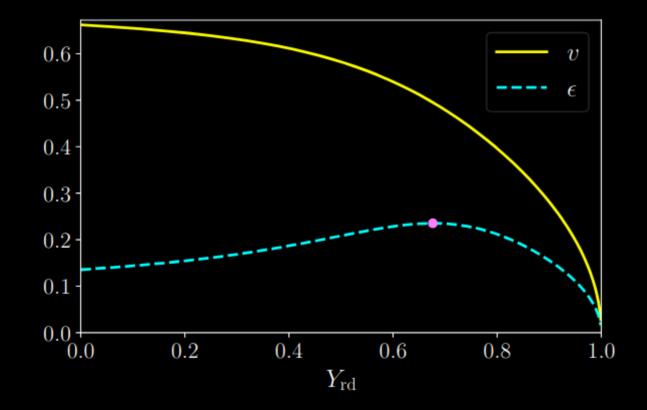
$$\dot{n}_l = \frac{\dot{\rho}_\ell}{\alpha L}$$

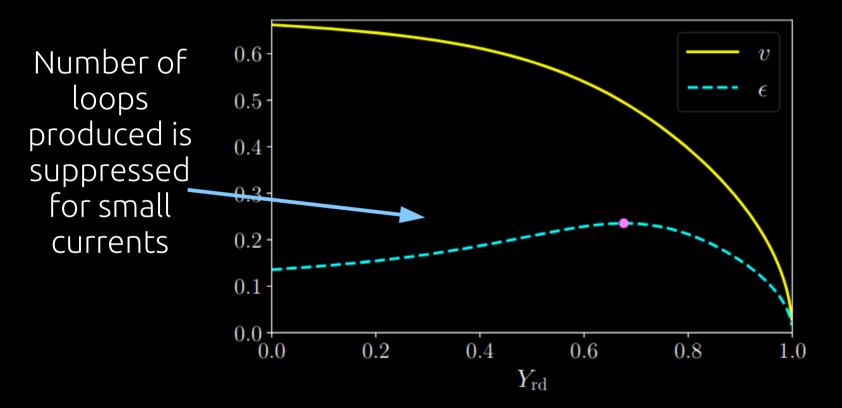
Martins, Peter, Rybak & Shellard 2021 (arXiv: 2011.09700 and arXiv: 2108.03147)

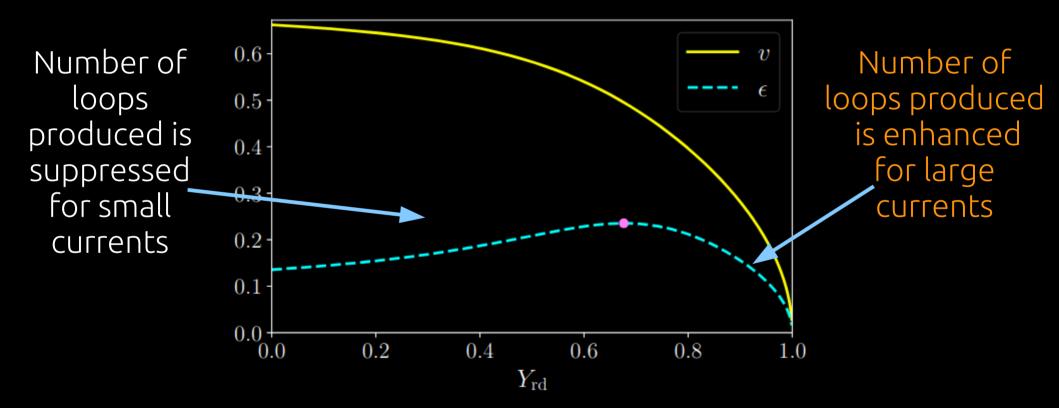
IN THE RADIATION ERA:

$$L_{\rm ph} = \xi_r t \quad \text{and} \quad v = v_r \,,$$

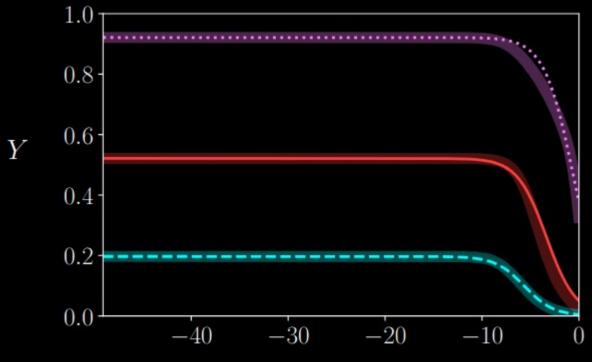
$$\xi_r^2 = (1 - Y)k(k + \tilde{c})$$
 and $v_r^2 = (1 - Y)\frac{k}{k + \tilde{c}}$







Current is quickly dissipated in the matter era



x

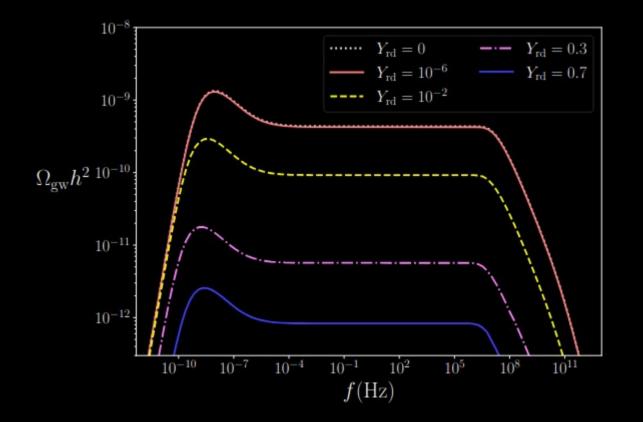
IN THE RADIATION ERA:

THE AMPLITUDE OF THE PLATEAU MAY BE SIGNIFICANTLY AFFECTED AND DEPENDS ON THE VALUE OF CURRENT

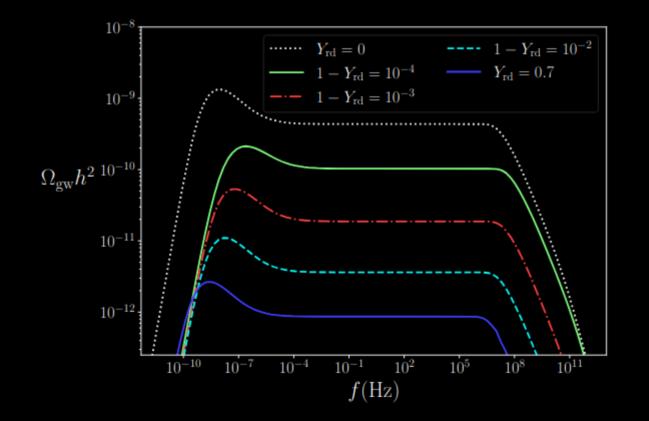
IN THE MATTER ERA:

THE CONTRIBUTION OF MATTER-ERA LOOPS IS (MOSTLY) UNNAFFECTED

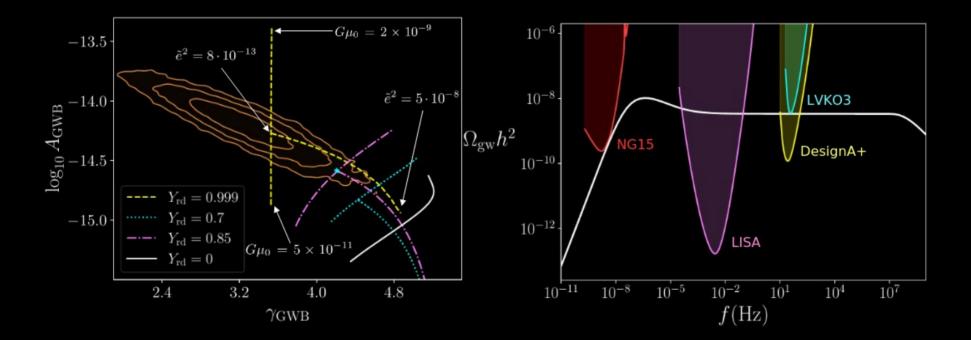
For small enough currents:



For large enough currents:



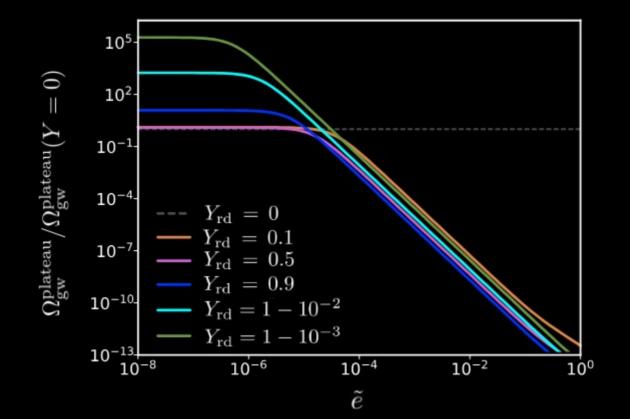
Superconducting strings with high current fit better NANOGrav data than standard cosmic strings



CURRENT MAY ACTUALLY HELP RECONCILE COSMIC STRINGS WITH NANOGRAV DATA!

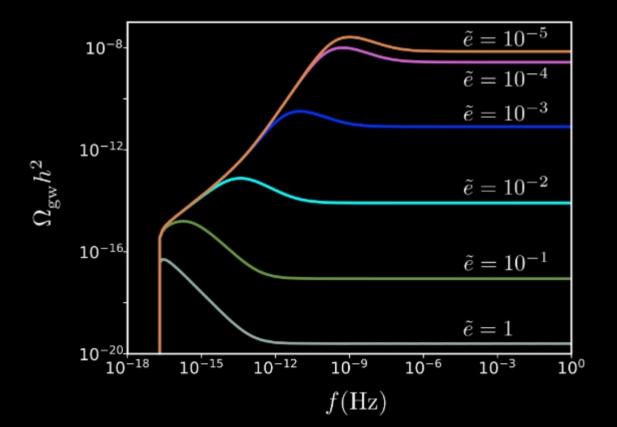
IMPACT OF CHARGE ON THE SGWB

As the charge of the current carriers increases, the amplitude is suppressed:



IMPACT OF CHARGE ON THE SGWB

But the shape of the spectrum is also affected



THERE MAY BE DISTINCTIVE SIGNATURES ON THE SGWB SPECTRUM GENERATED BY STRINGS, WHICH MAY ALLOW US TO PROBE THE UNDERLYING PARTICLE PHYSICS SCENARIO

TO SUM UP

*Current may significantly decrease the efficiency of emission of gravitational radiation by cosmic strings and affect the spectrum of emission;

*The amplitude of the SGWB for chiral superconducting strings is highly dependent on the value of current and on the charge of current carriers;

*There may also be significant changes to the shape of the spectrum if the charge of current carriers is large enough;

THANKS!